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Fundamental Concepts of Generative Machine Learning

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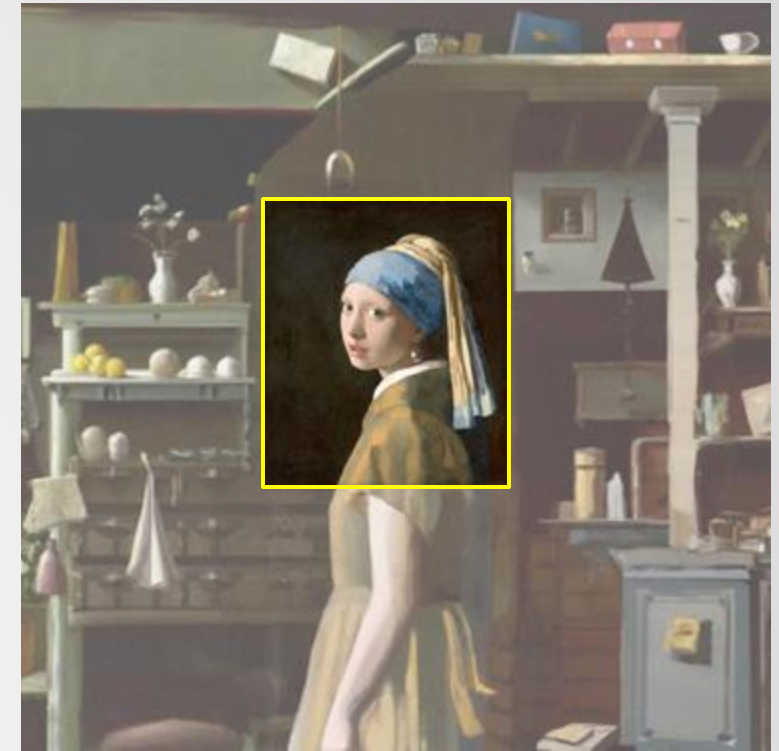
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Lesson 1: Mathematical Background

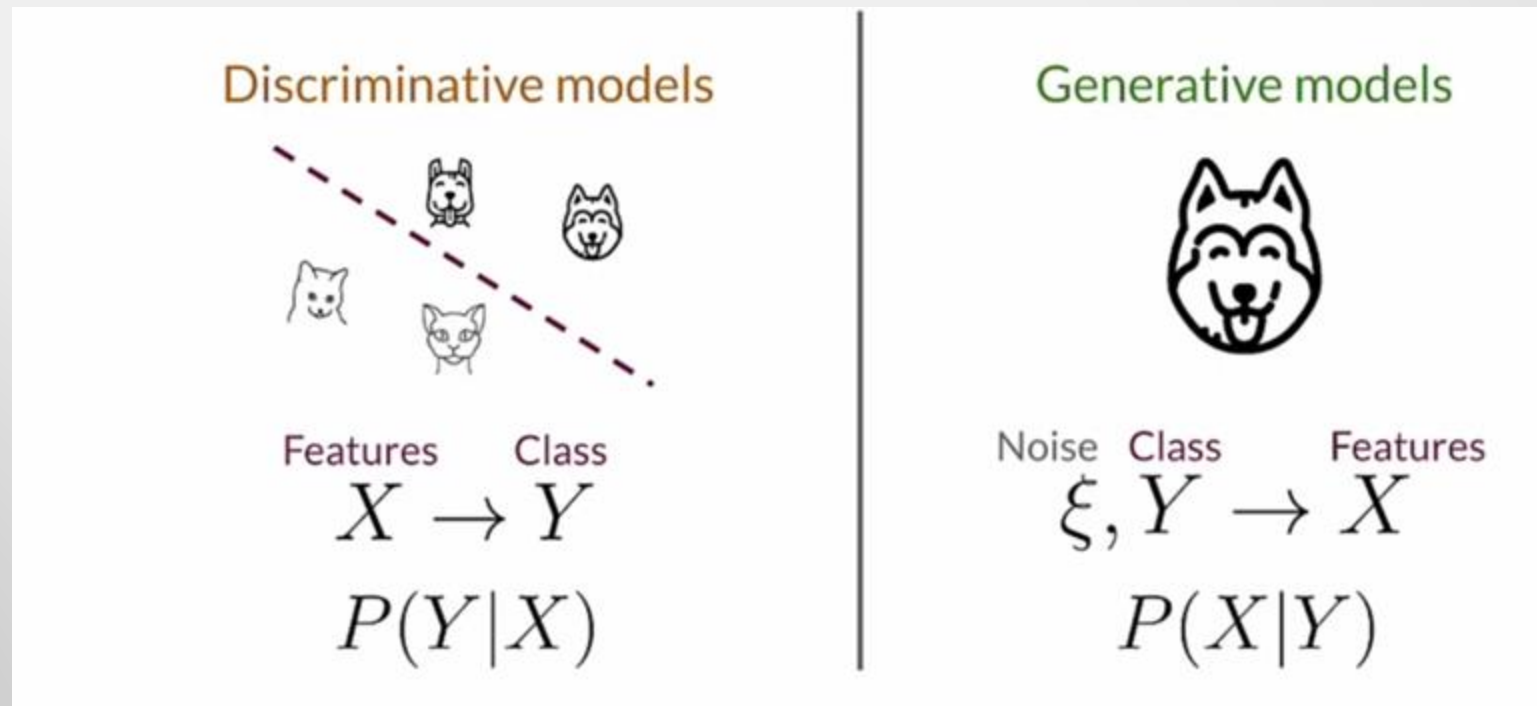
Welcome to Part I: “Mathematical Background”

This part includes four subsections:

- **Generation vs. Discrimination in Machine Learning**
- Data Distribution, Sampling, Inference and Generation
- Expectation and Likelihood
- Evaluation for Generative Models, Distribution Distances, Divergence and Entropy

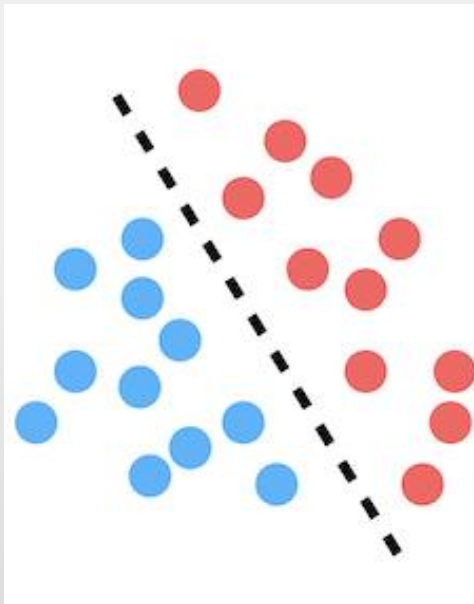


Discriminative vs Generative Models



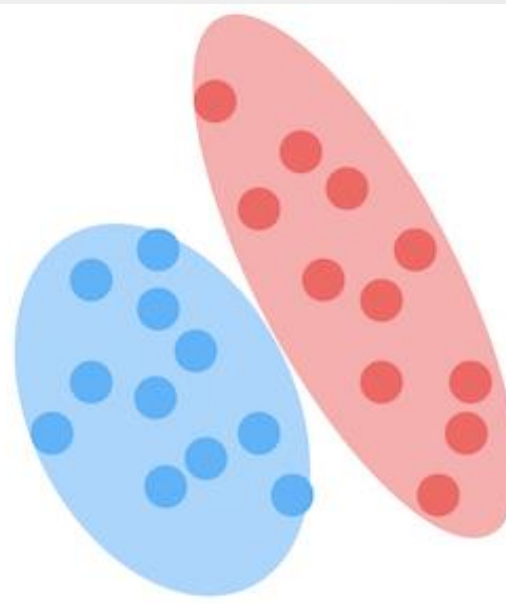
Discriminative vs Generative Models

Discriminative models



“decision boundary”

Generative models



“distribution”

- Logistic regression
- Scalar Vector Machine
- Neural networks (CNNs)
- etc

- Naïve Bayes
- Bayesian networks
- Markov random fields
- Hidden Markov Models
- Gaussian Mixture Models
- etc

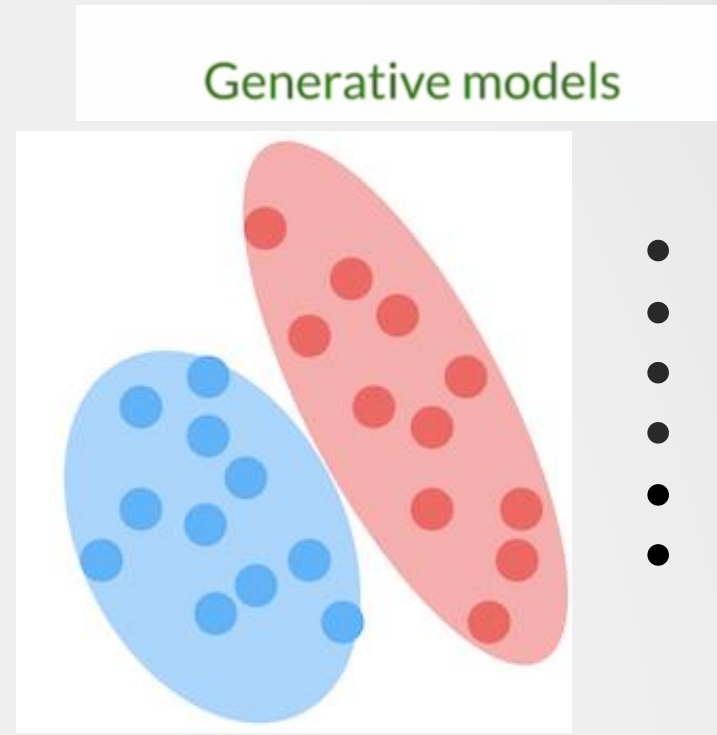
Before the age of GANs, conventional ML scrutinised classifiers into these two categories.

Generative Classifier

A “generative classifier” is a statistical model of the joint probability distribution:

$$P(X, Y)$$

- on given observable variable **X**
 - Observation $\stackrel{\text{def}}{=} \text{Feature}$
- and target variable **Y**



“distribution”

- Naïve Bayes
- Bayesian networks
- Markov random fields
- Hidden Markov Models
- Gaussian Mixture Models
- etc

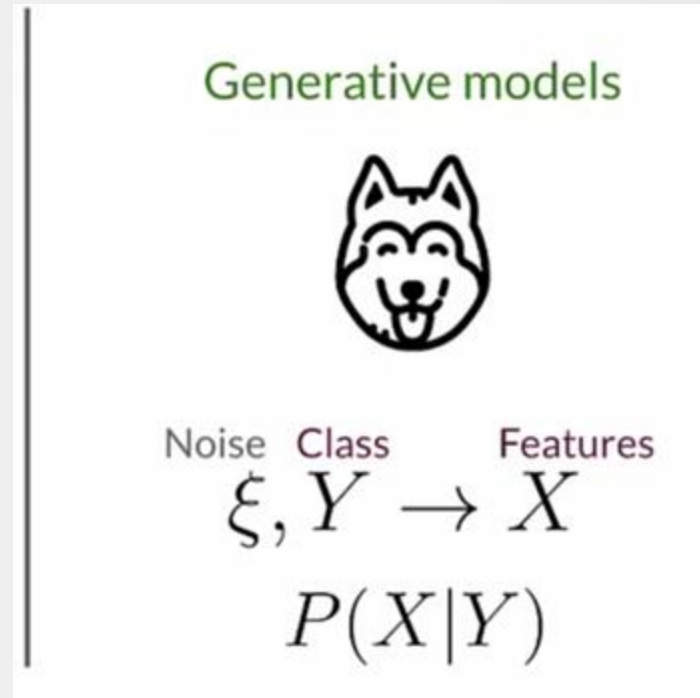
Generative Classifier (vs Generation)

A “generative classifier” is a statistical model of the joint probability distribution:

$$P(X, Y)$$

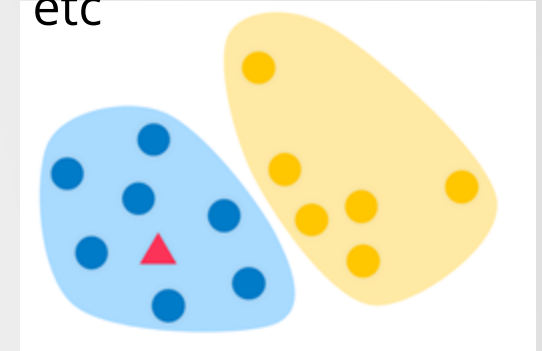
- on given observable variable \mathbf{X}
 - Observation $\stackrel{\text{def}}{=} \text{Feature}$
- and target variable \mathbf{Y}

“When a new observation is fed to a generative classifier, it tries to predict which class would have most likely generated the given observation.”



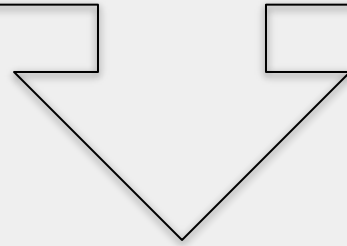
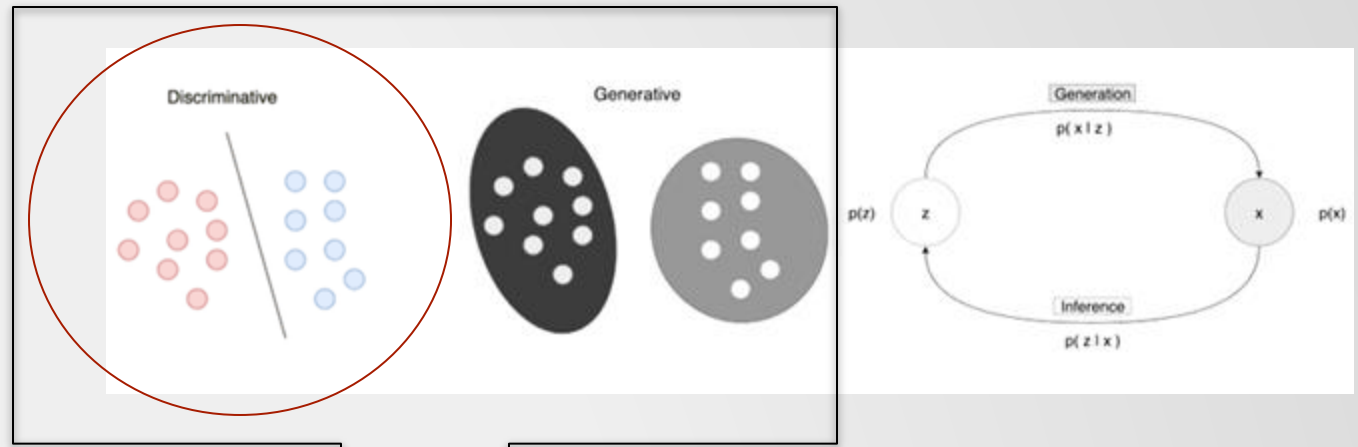
“distribution”

- Naive Bayes
- Bayesian networks
- Markov random fields
- Hidden Markov Models
- Gaussian Mixture Models
- etc



Classification vs Generation

Discriminative models (or classifiers) are machine learning models that learn to classify input data into different categories based on a set of features.

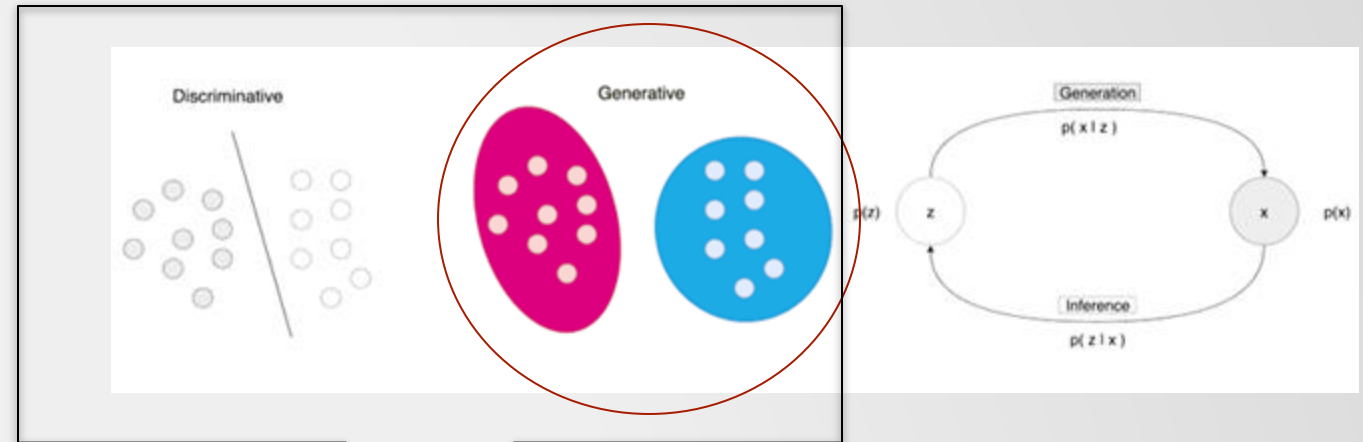


classifiers

These models learn to distinguish between different classes of data **without necessarily modeling the underlying probability distribution of the data.**

Classification vs Generation

Generative classifiers are models that **learn to model the probability distribution of the input data for each class separately, and then use Bayes' rule to calculate the posterior probability of each class given the input.**



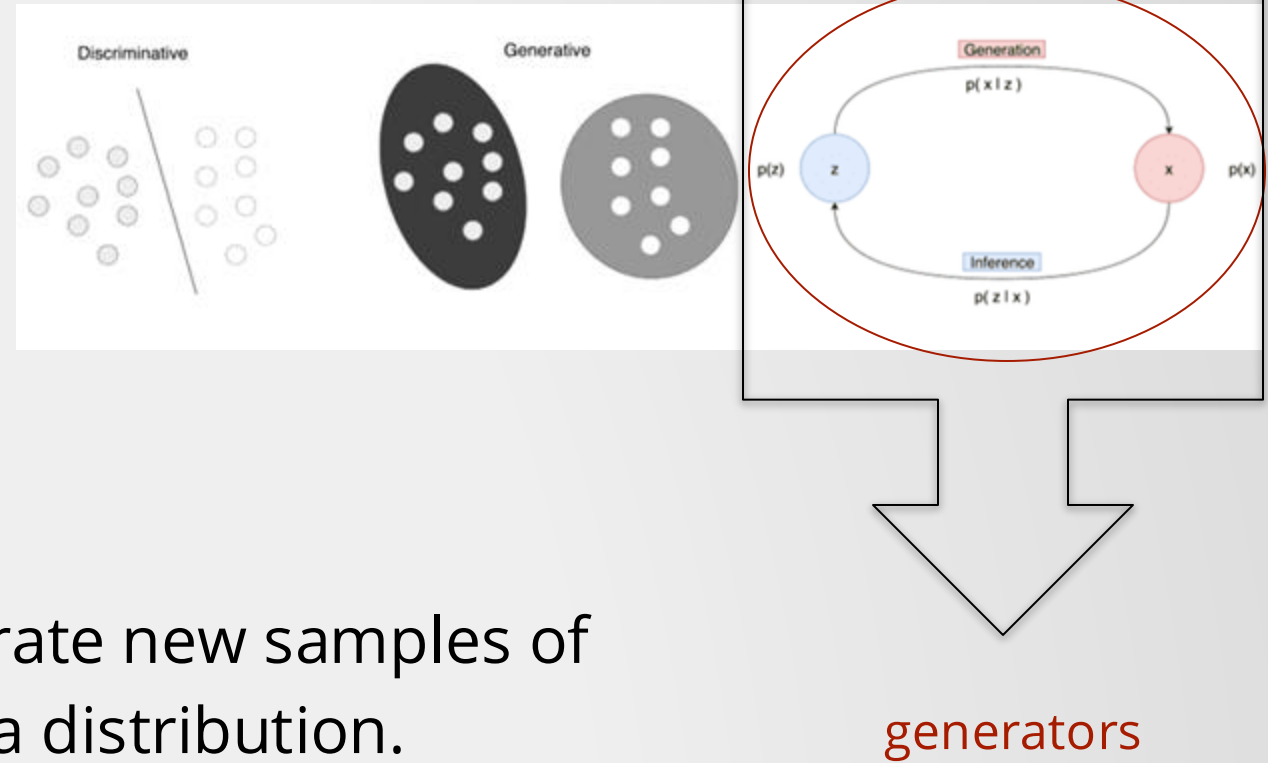
classifiers

These models can be used to classify new data points into different categories based on their likelihood under each class distribution.

Classification vs Generation

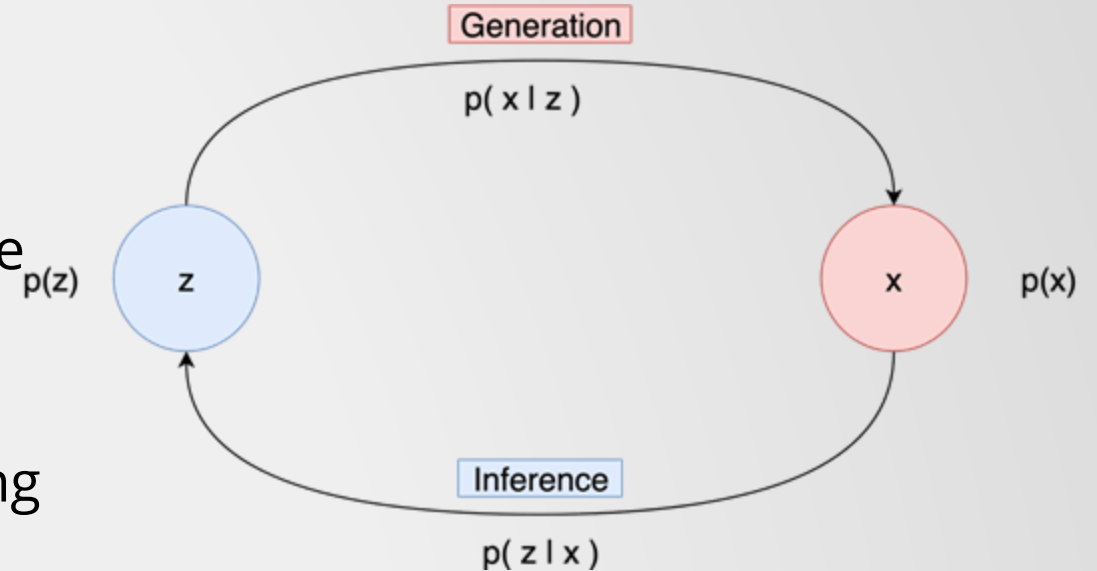
Generative (or generation) models are machine learning models that learn to model the probability distribution of the input data.

These models can be used to generate new samples of data that resemble the original data distribution.



Generation

- $p(z)$: a noise distribution (i.e. latent space)
- $p(x/z)$: is the generation process, i.e. the generation of a new sample x , given a noise vector z
- $p(x)$: is the data/observation distribution.
- $p(z/x)$: is the inference process, i.e. extracting the noise vector z that would generate the sample x .



Next lecture:

Part I: “Mathematical Background”

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Thanks



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