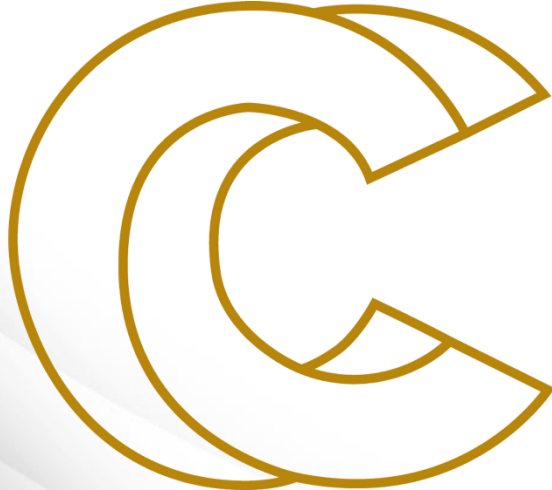




EURO^{4SEE}

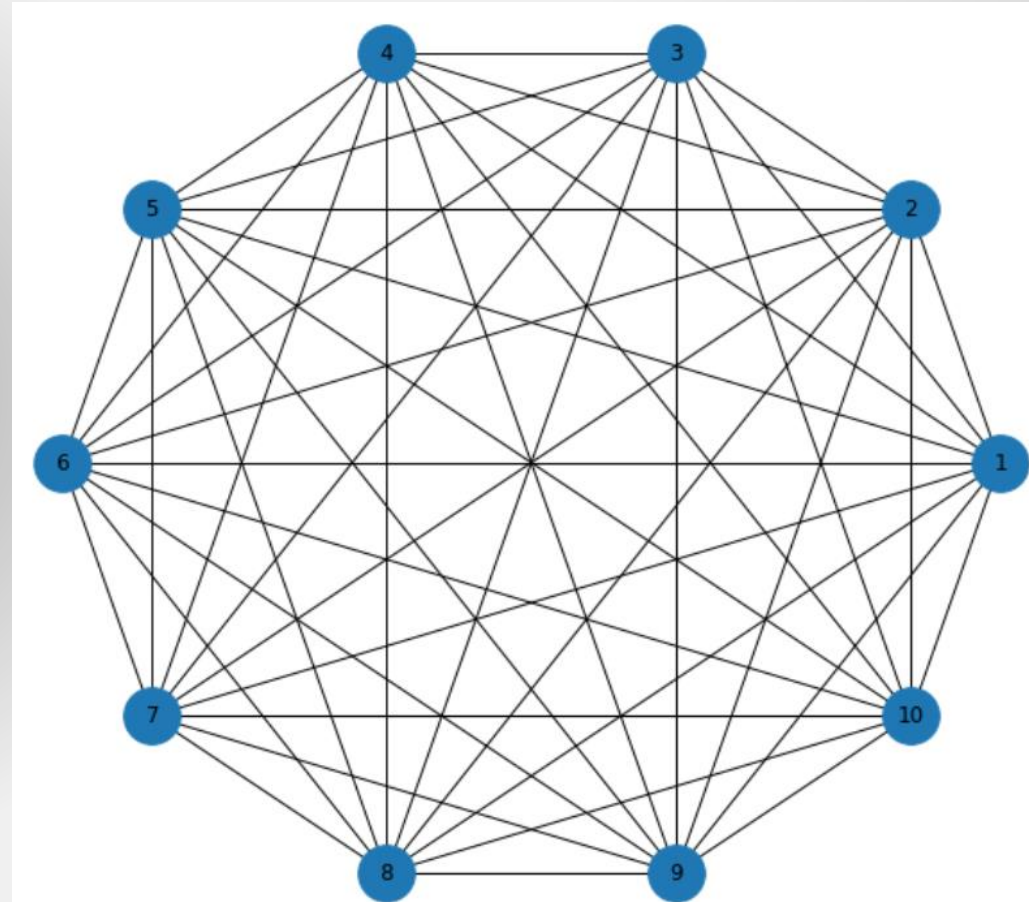
Residue Networks: Understanding the Time Evolution and Mutations of
Proteins from a Graph Theoretical Perspective

Tandac Furkan Guclu
Sabancı University

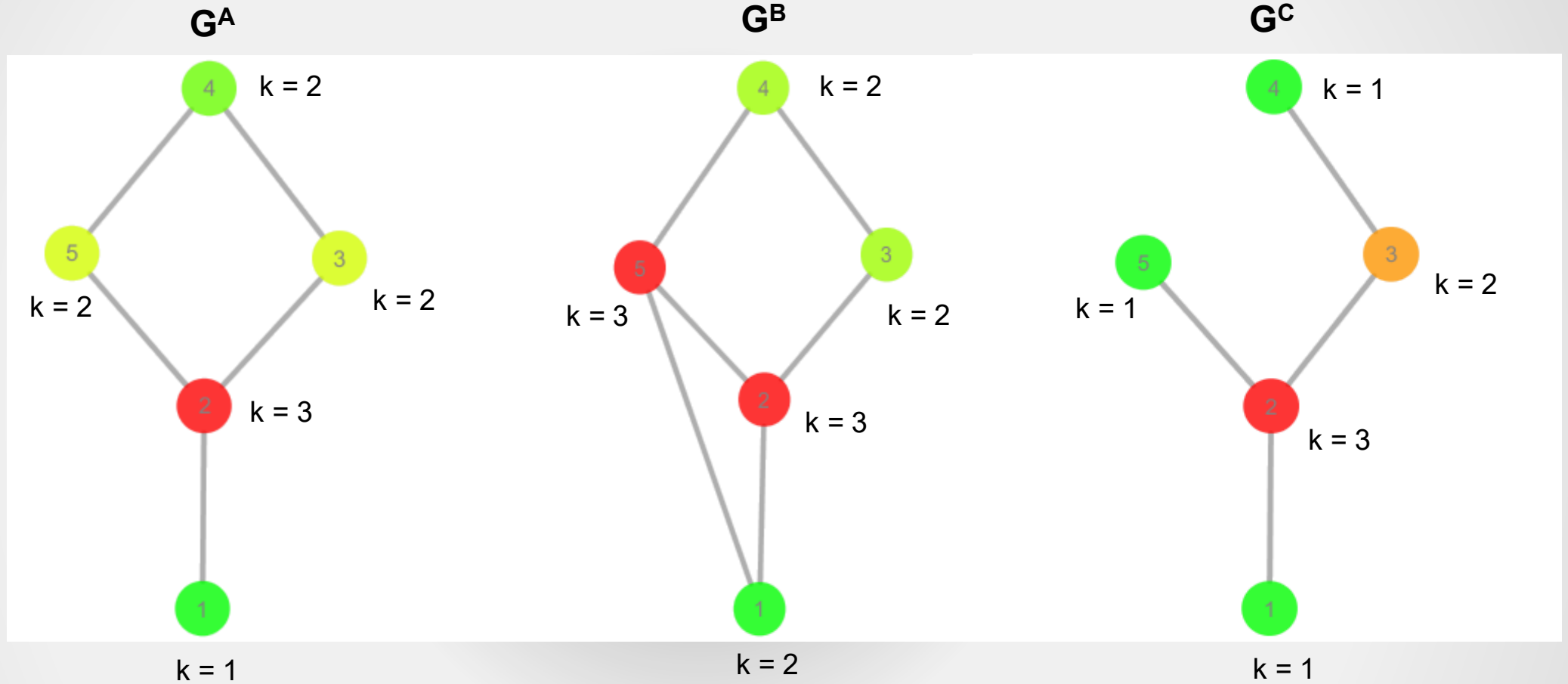
Lesson 1: Introduction to graphs and measures

Graph or network

- Consists of vertices (nodes) and edges (links)
- Nodes and edges may be weighted
- Stored as adjacency matrix or edge/node list
- Here our graphs are
 - Undirected
 - Unweighted
 - No self-loops
 - No parallel edges
- Parameters we use
 - Degree or number of neighbors (k)
 - Average shortest path length ($\langle L \rangle$)
 - Clustering coefficient (C)
 - Betweenness centrality (BC)



Degree or number of neighbors (k)



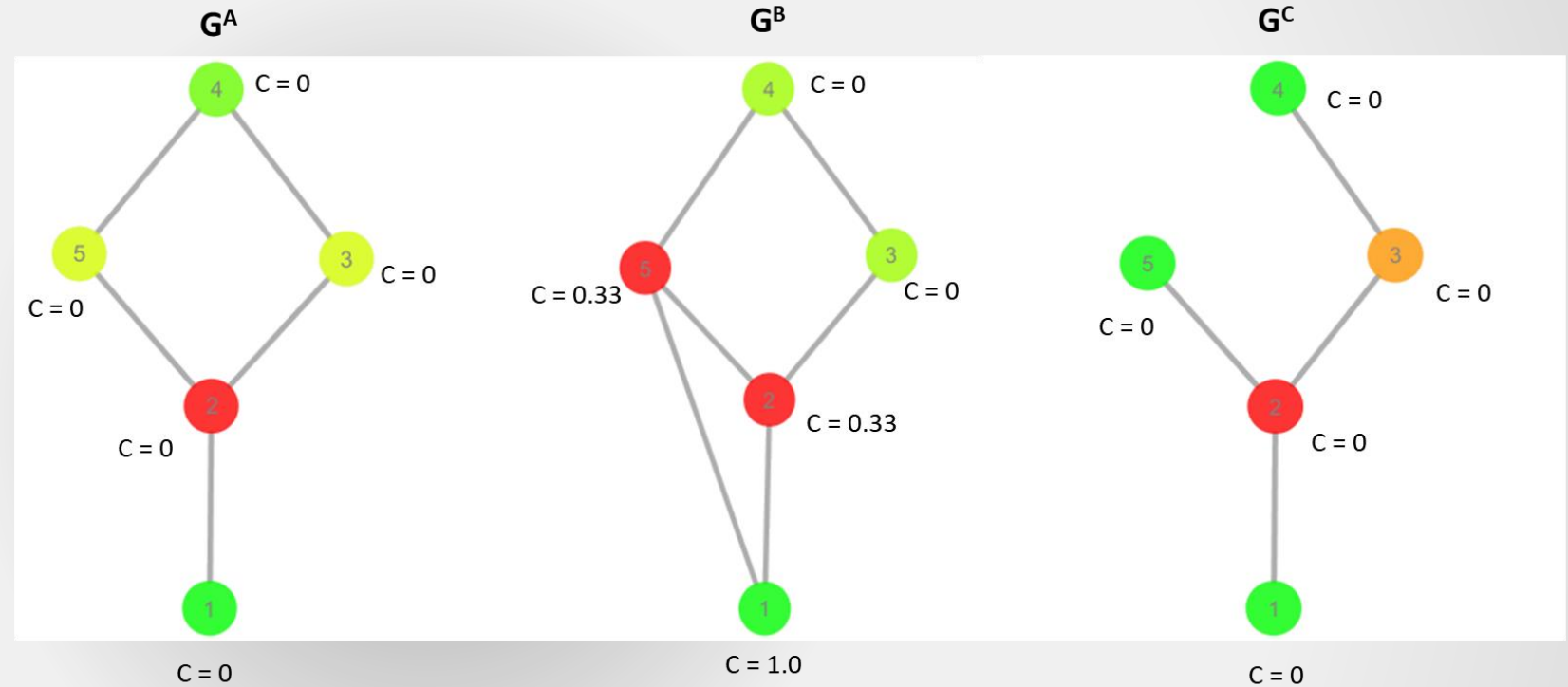
Local information about network.

Clustering coefficient (C)

For G^B :

$$C = \frac{2T(u)}{k(u)(k(u) - 1)}$$

$$C_{Node2} = \frac{2 \times 1}{3 \times 2} = 0.33$$



Connectivity of the neighbors of a node, semi-local information about connectivity.

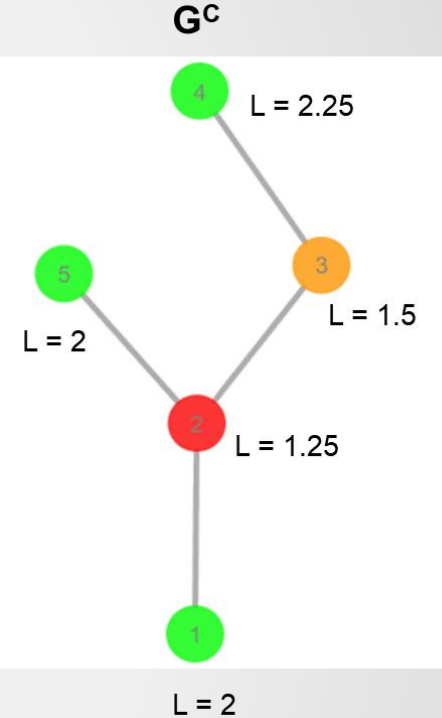
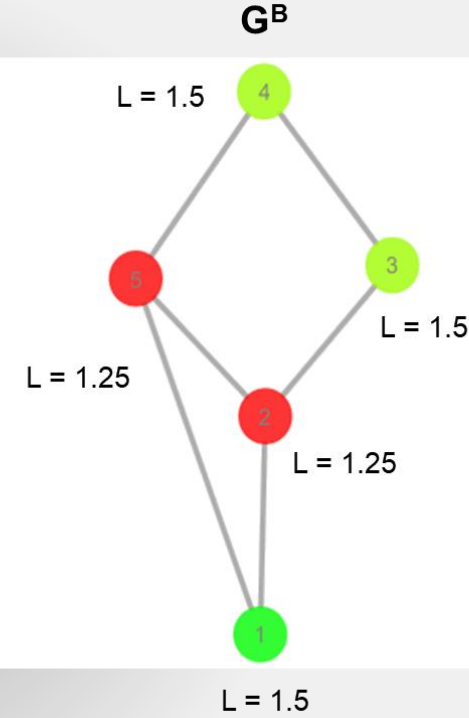
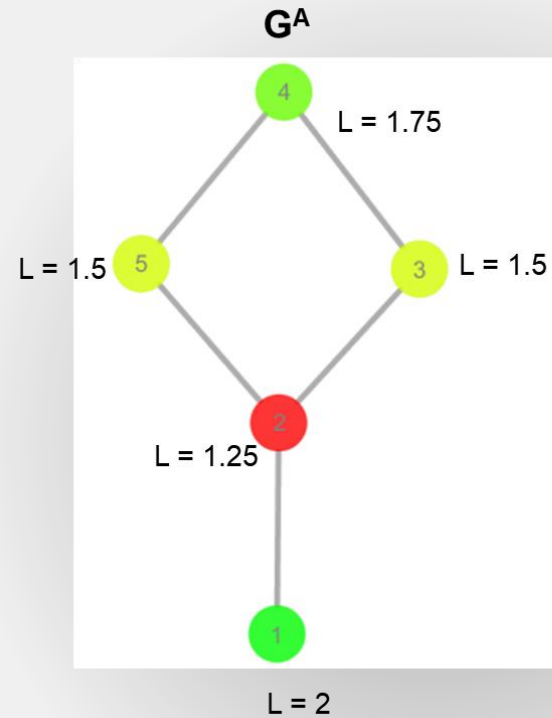
Average Shortest Path Length (<L>)

For G^A :

$$\langle L_i \rangle = \frac{1}{n-1} \sum_i L_{ij}$$

$$\langle L \rangle_{Node\ 2} = \frac{L_{21} + L_{25} + L_{23} + L_{24}}{N}$$

$$\langle L \rangle_{Node\ 2} = \frac{1 + 1 + 1 + 2}{4} = 1.25$$



Information about the accessibility of a node in units of edges.

Betweenness centrality (BC)

For G^A :

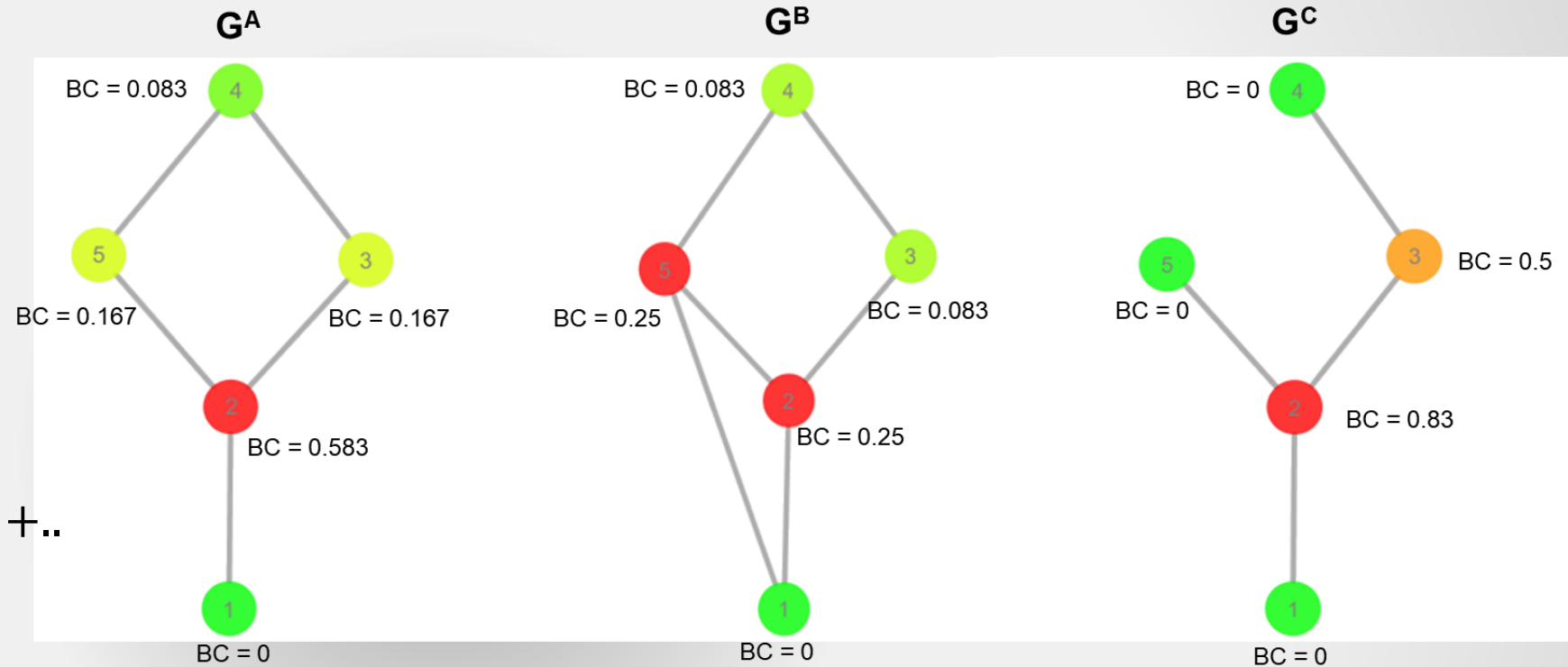
$$BC(X) = \sum \left(\frac{P(a,b|X)}{P(a,b)} \right)$$

$$BC_{Node\ 2} = \frac{P_{13}(2)}{P_{13}} + \frac{P_{15}(2)}{P_{15}} + \frac{P_{14}(2)}{P_{14}} + ..$$

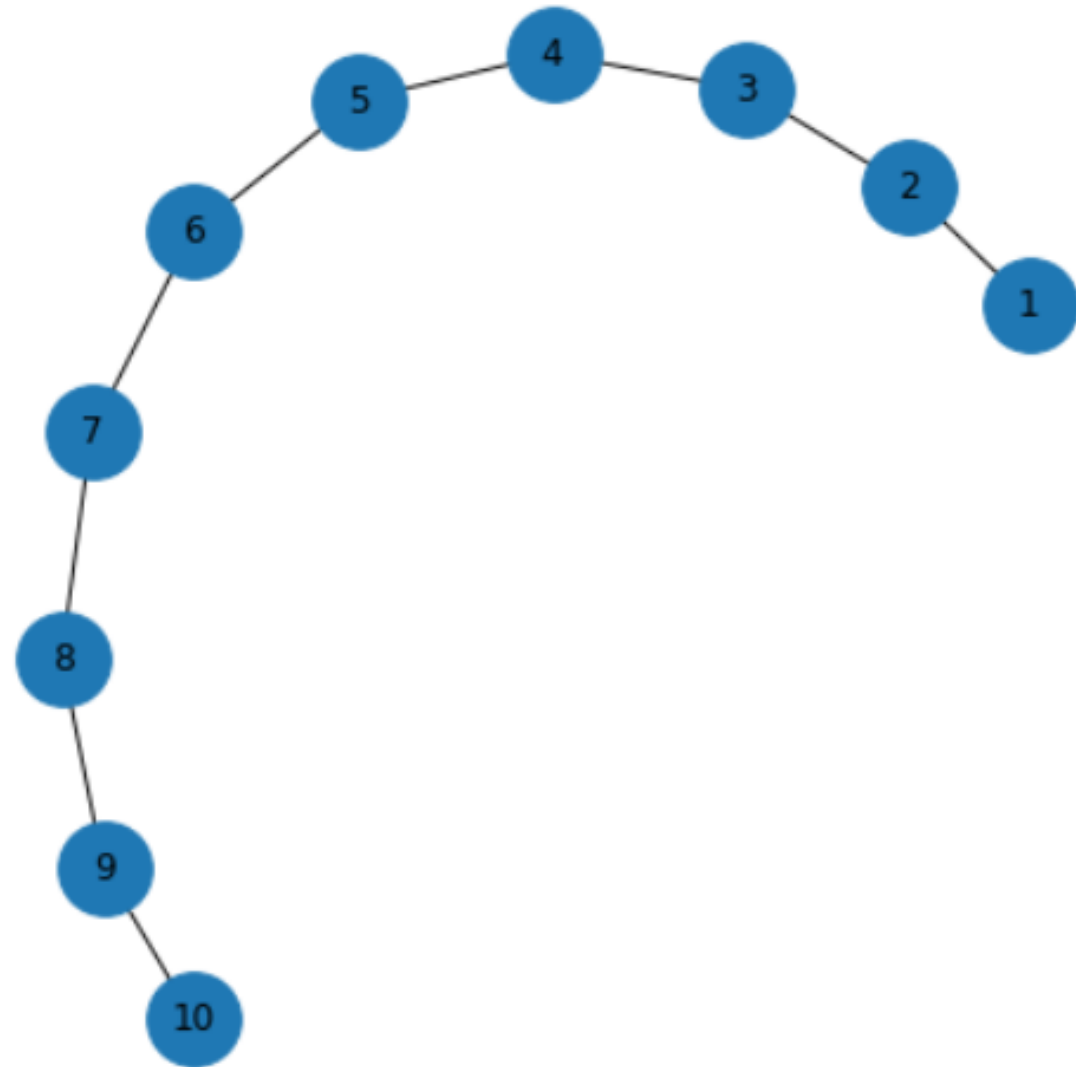
$$BC_{Node\ 2} = \frac{1}{1} + \frac{1}{1} + \frac{2}{2} + 0 + \frac{1}{2} + 0 = 3.5$$

Further normalized by $(n-1)(n-2)/2$

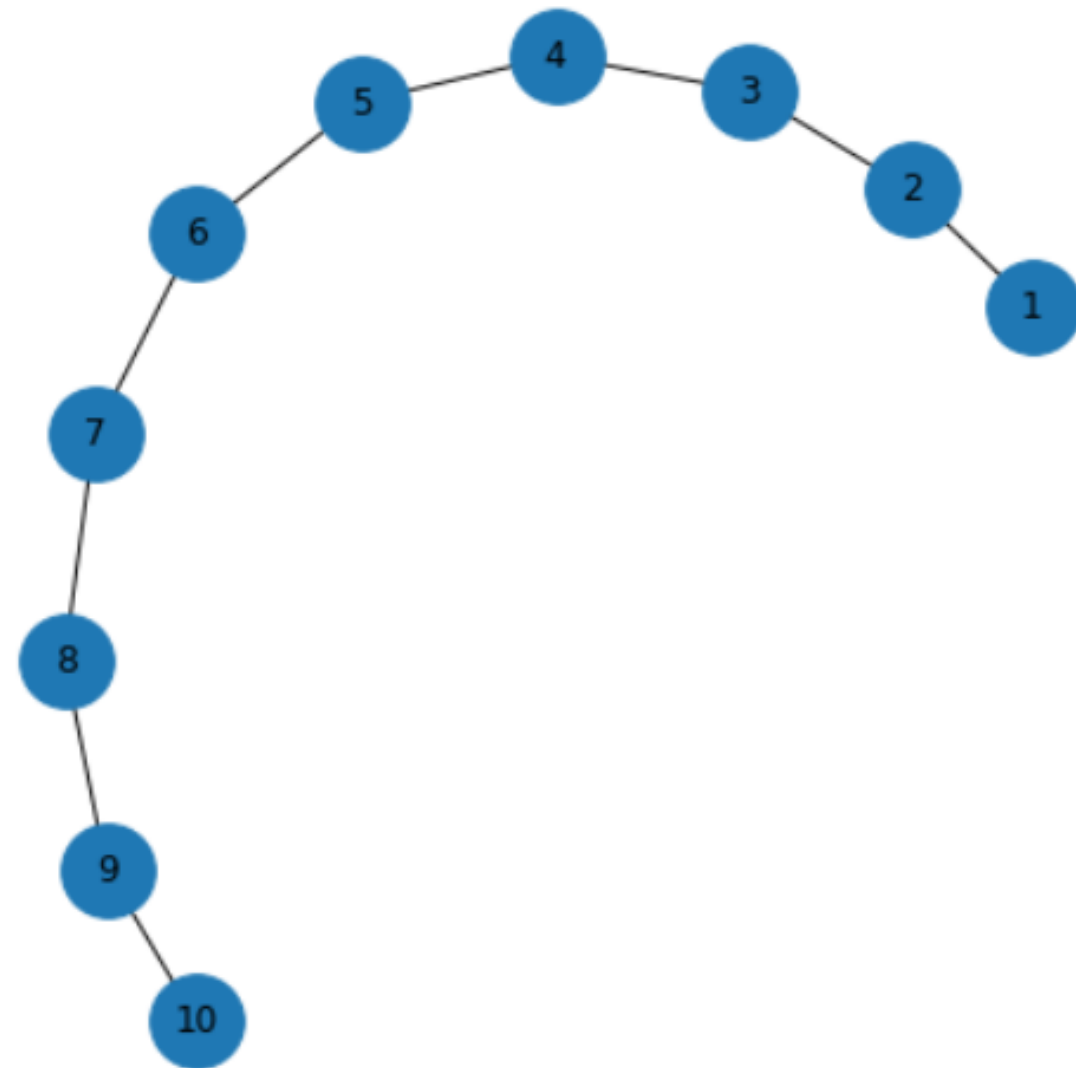
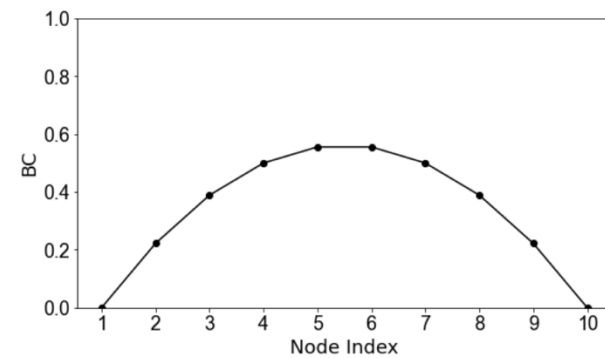
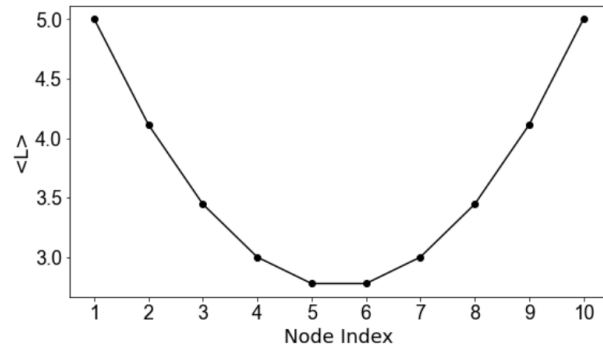
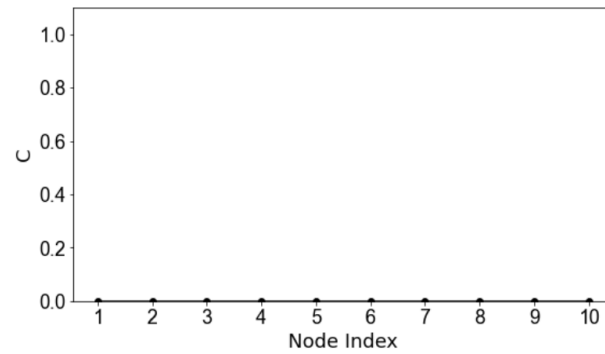
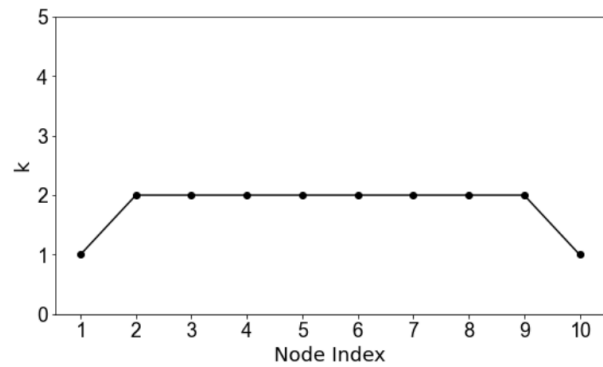
$$BC_{Node\ 2} = \frac{3.5}{6} = 0.583$$



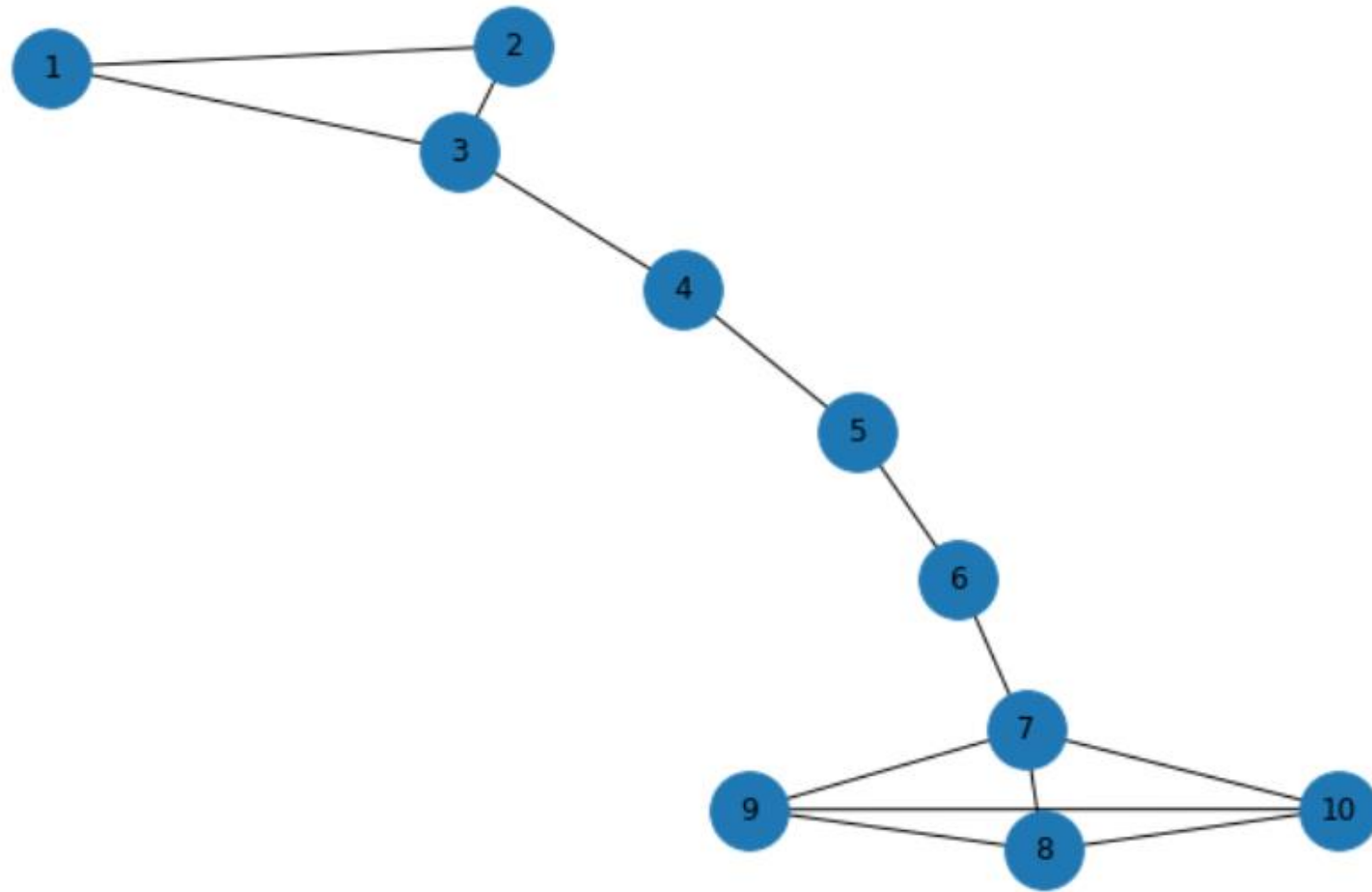
More toy graphs...



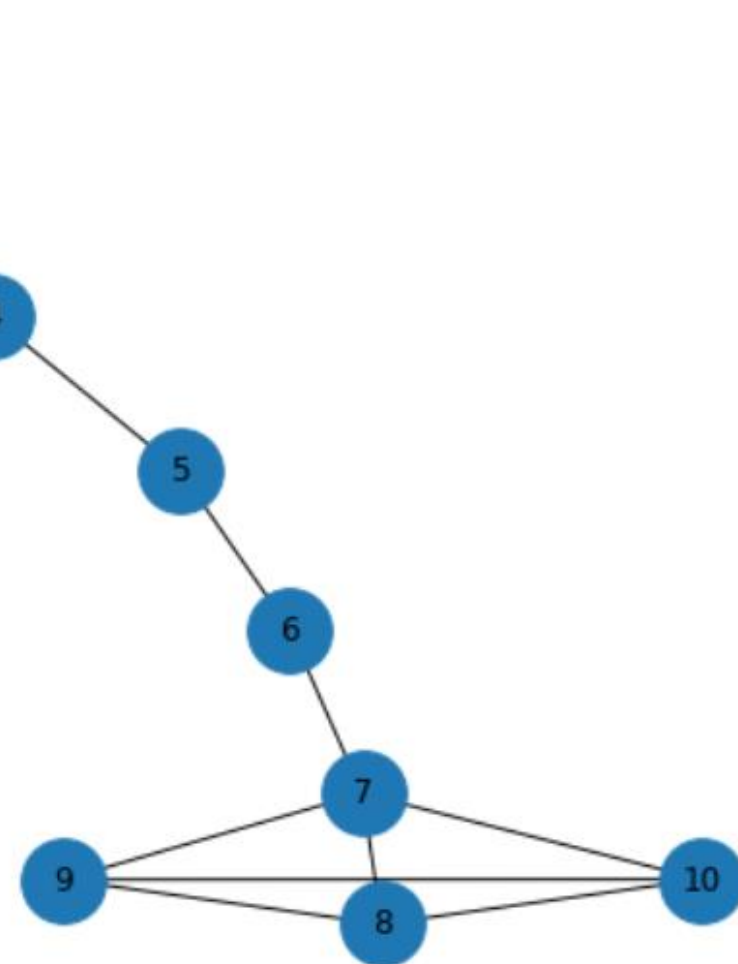
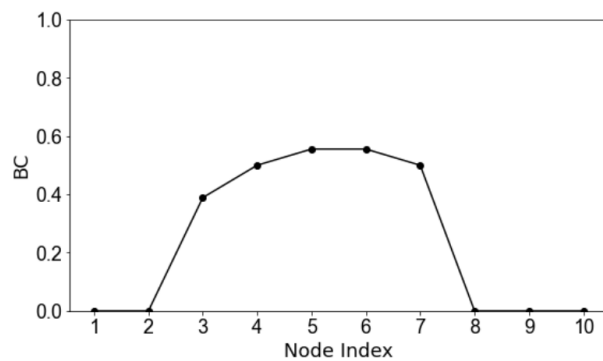
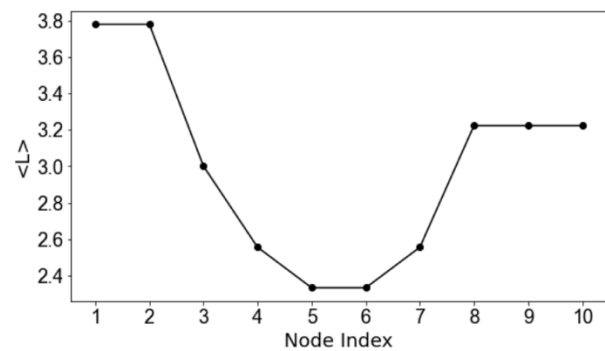
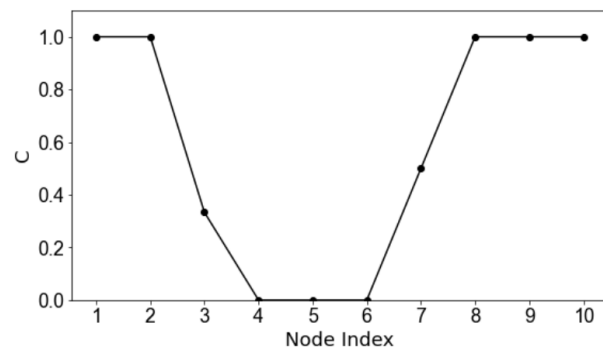
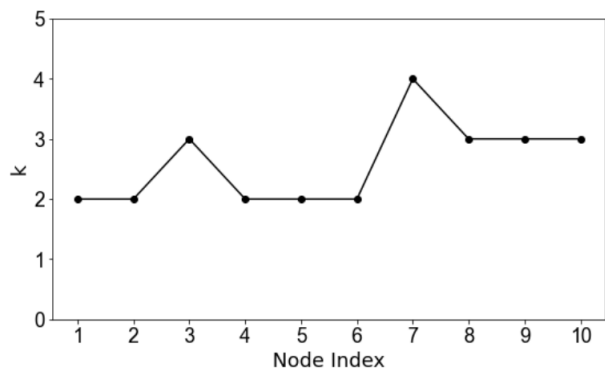
Number of nodes: 10
Number of edges: 9
Average degree: 1.8



Number of nodes: 10
Number of edges: 9
Average degree: 1.8

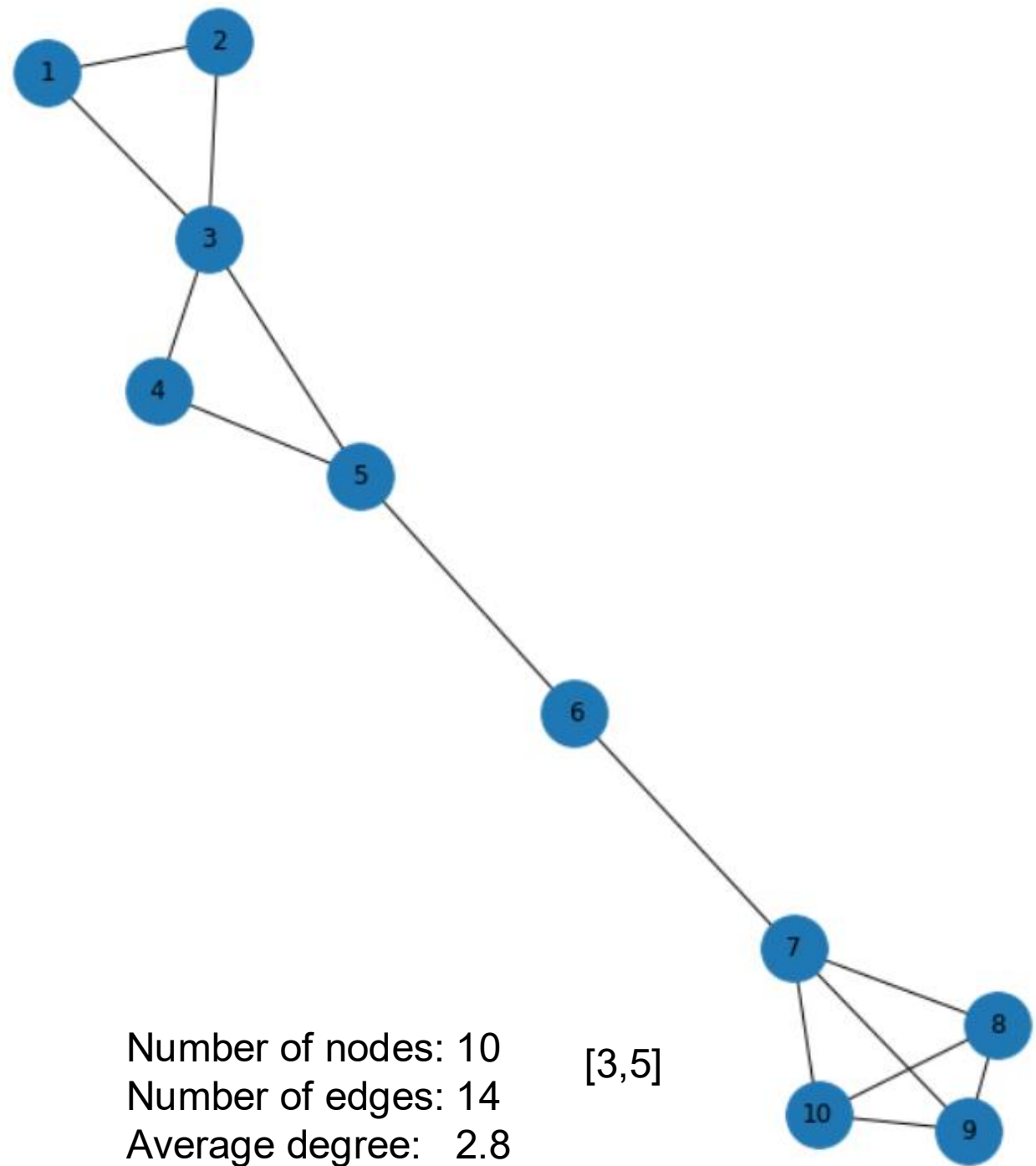


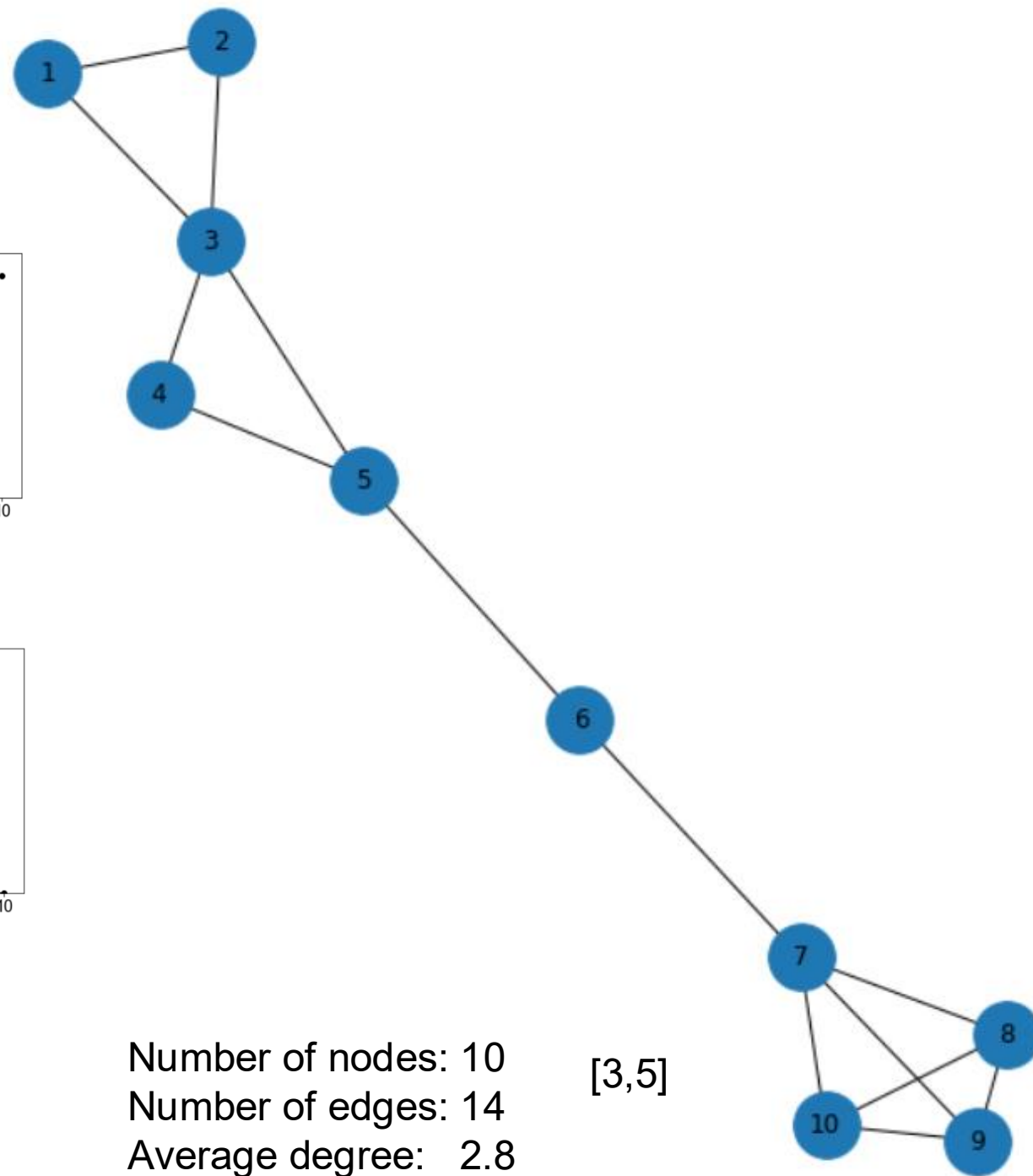
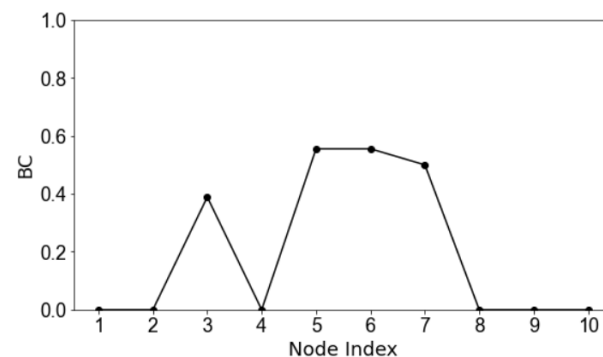
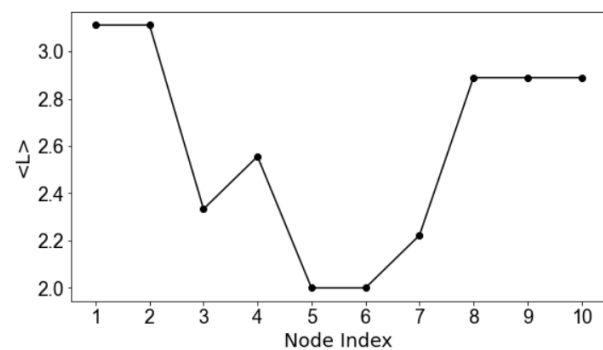
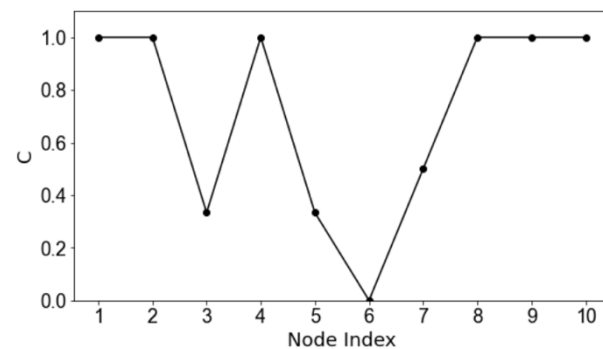
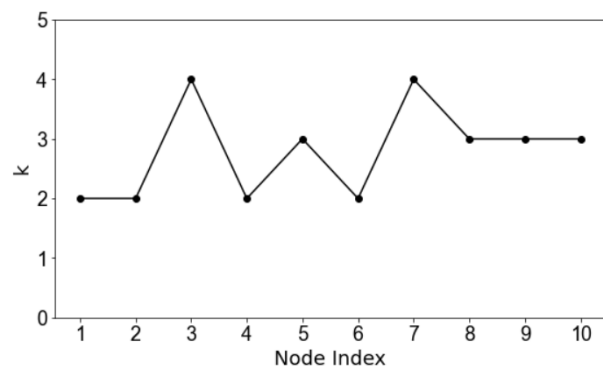
	[1,3]
Number of nodes: 10	[8,10]
Number of edges: 13	[7,10]
Average degree: 2.6	[7,9]



Number of nodes: 10
 Number of edges: 13
 Average degree: 2.6

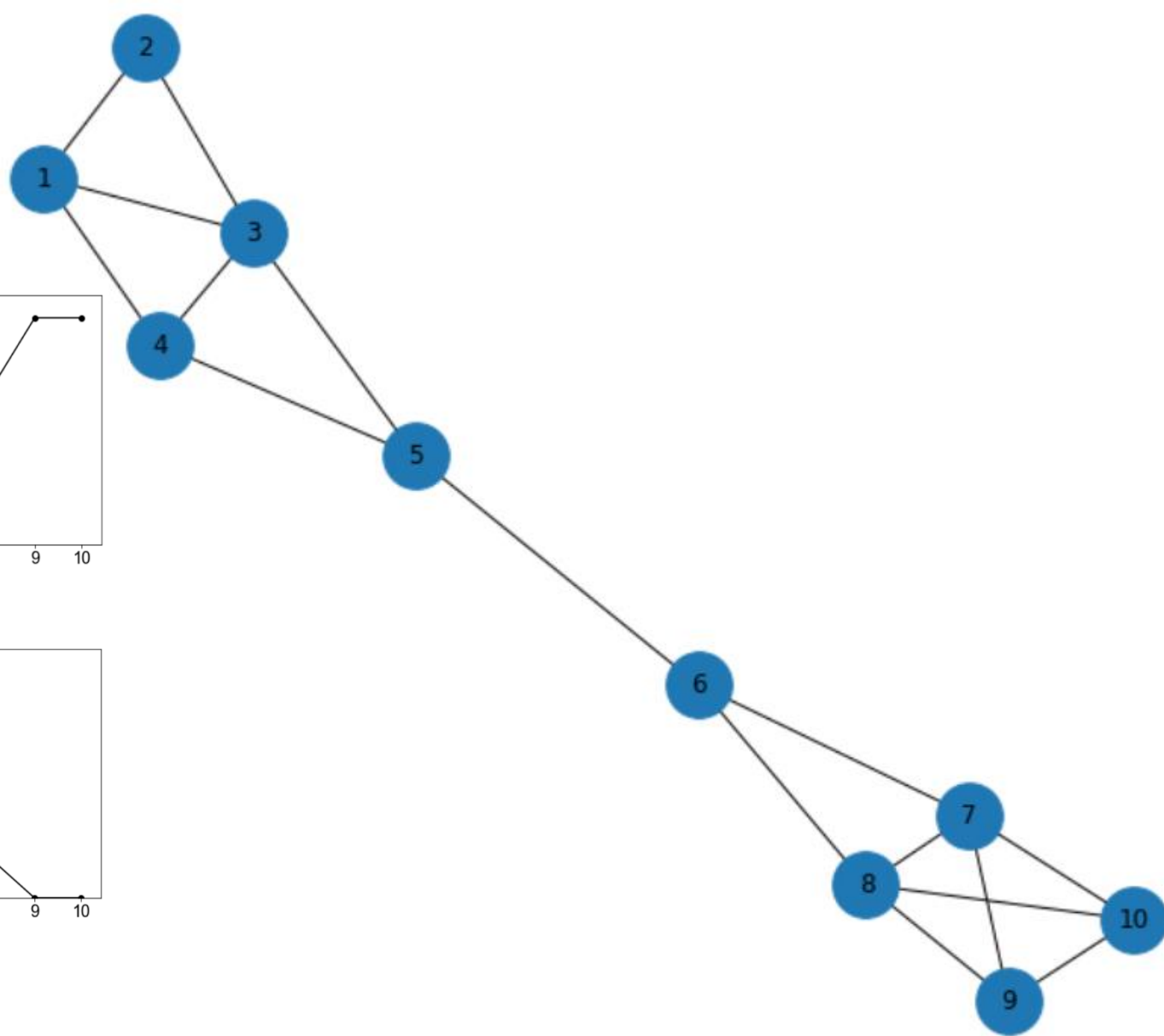
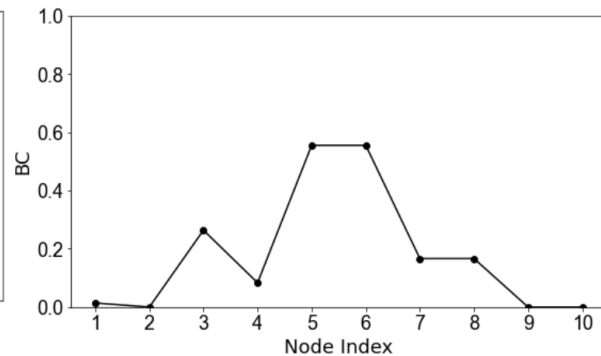
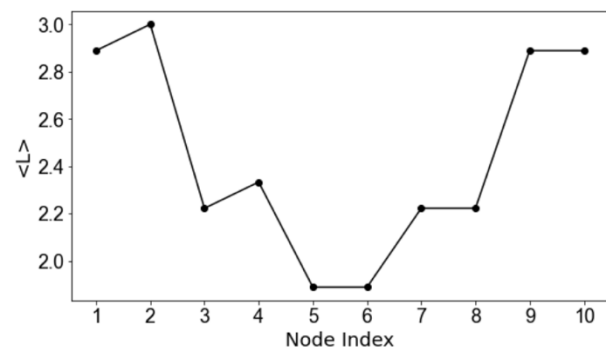
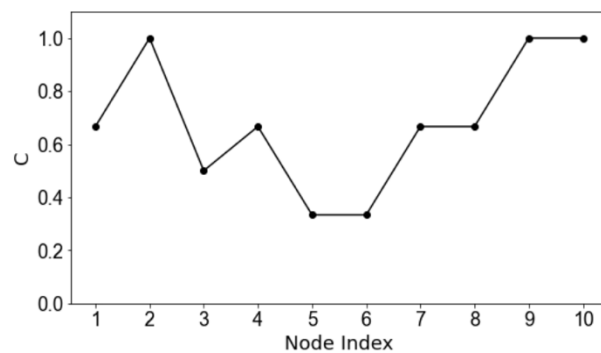
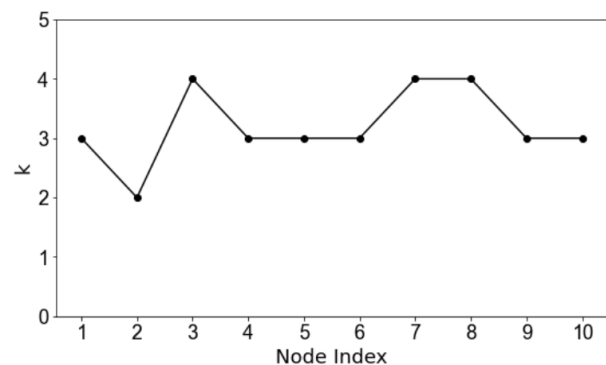
[1,3]
 [8,10]
 [7,10]
 [7,9]





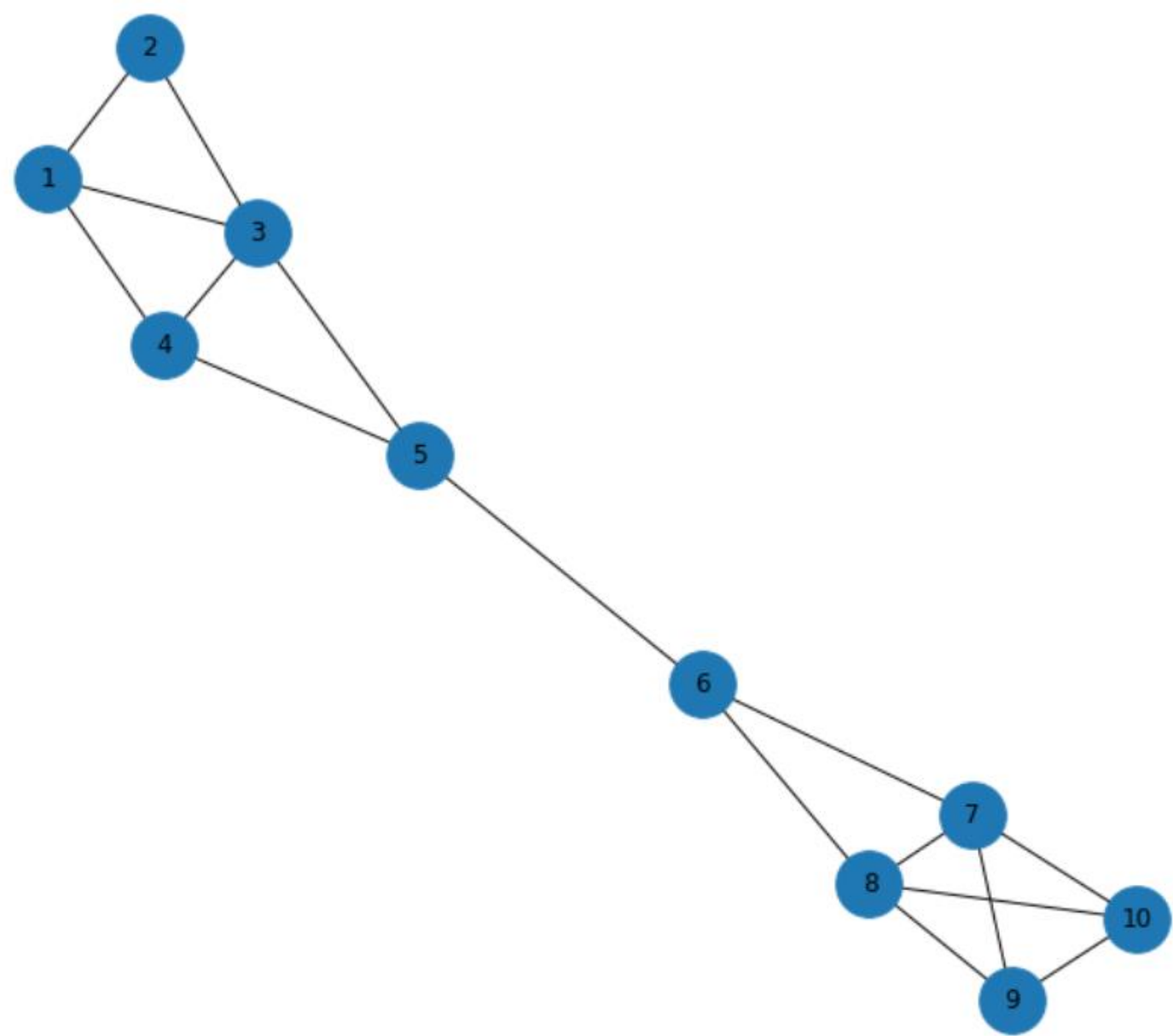
Number of nodes: 10
 Number of edges: 14
 Average degree: 2.8

[3,5]



Number of nodes: 10
 Number of edges: 16
 Average degree: 3.2

[1,4]
 [6,8]



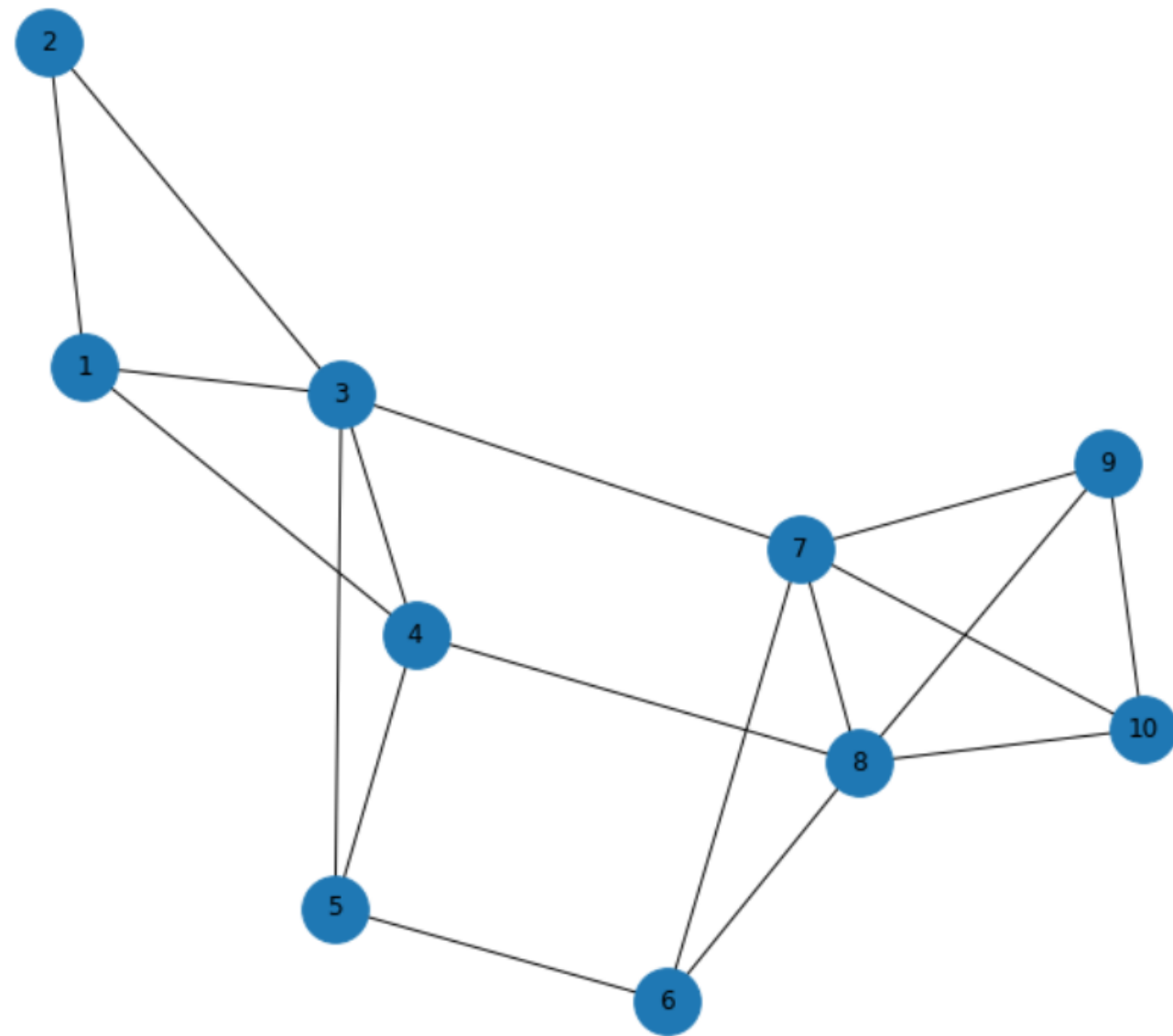
Number of nodes: 10

Number of edges: 16

Average degree: 3.2

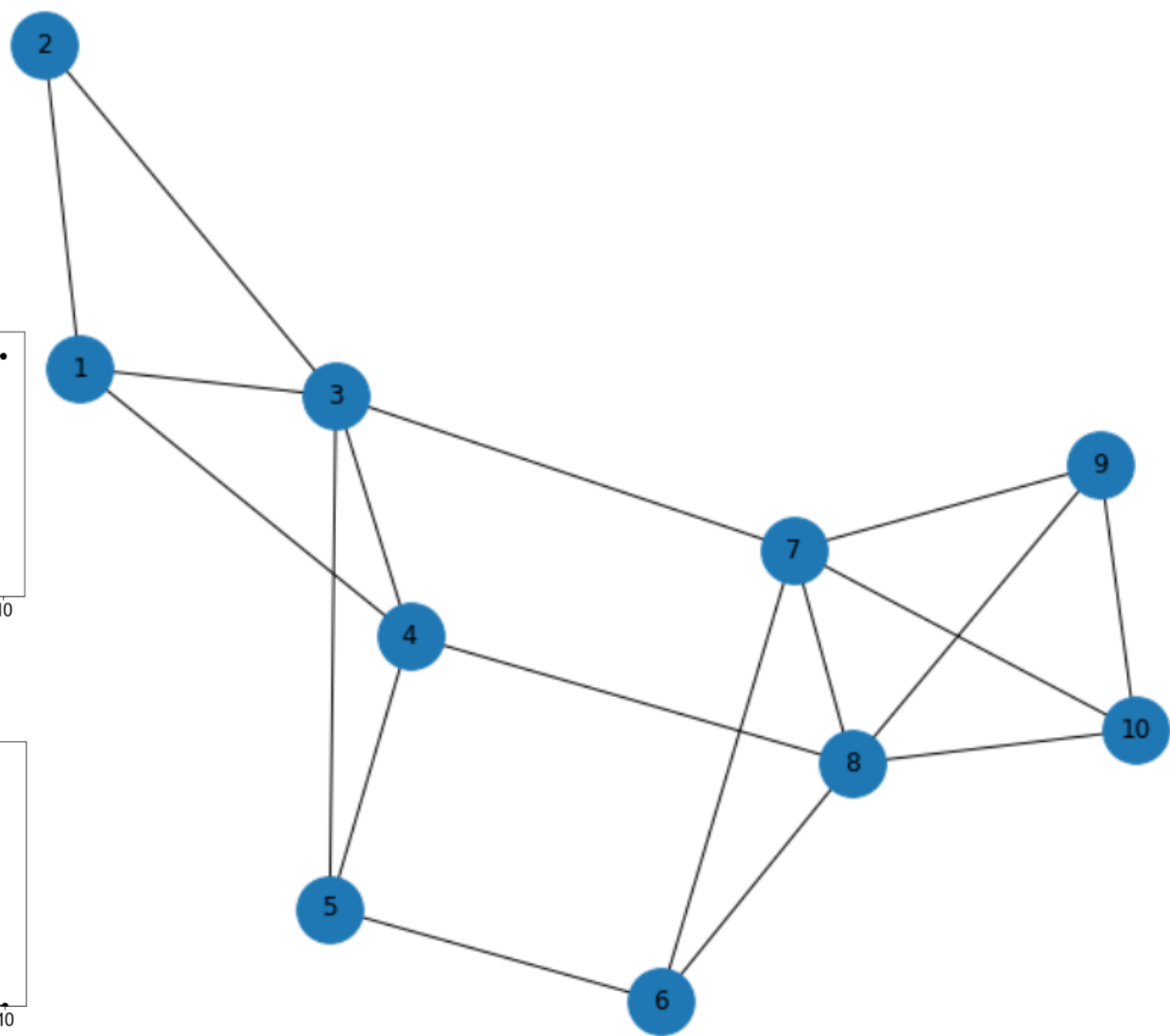
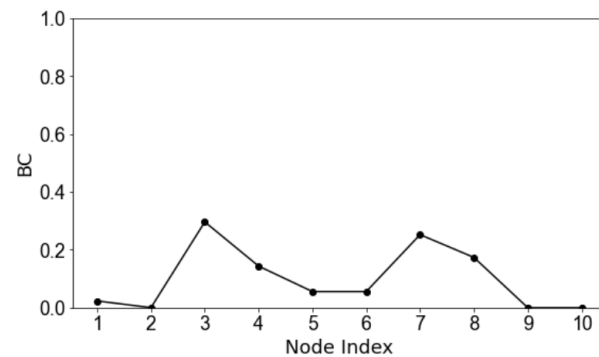
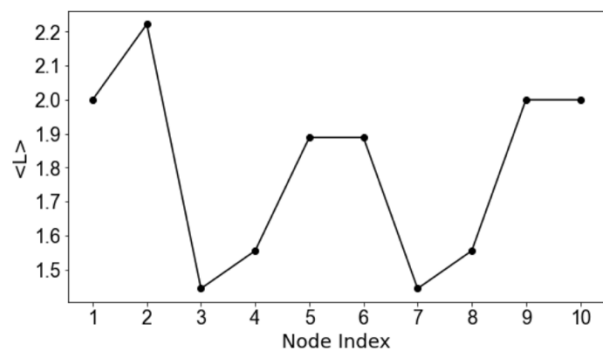
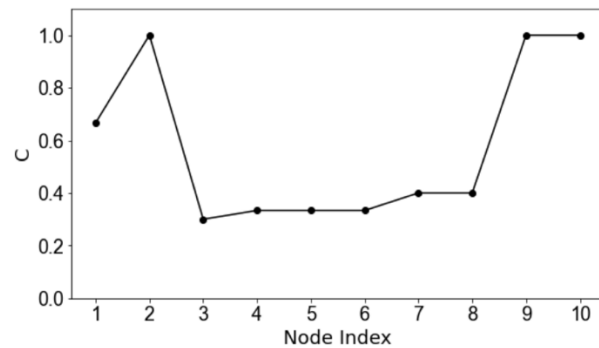
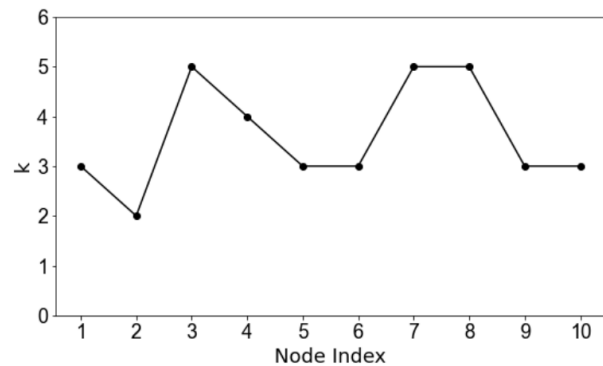
[1,4]

[6,8]



Number of nodes: 10
Number of edges: 18
Average degree: 3.6

[3,7]
[4,8]



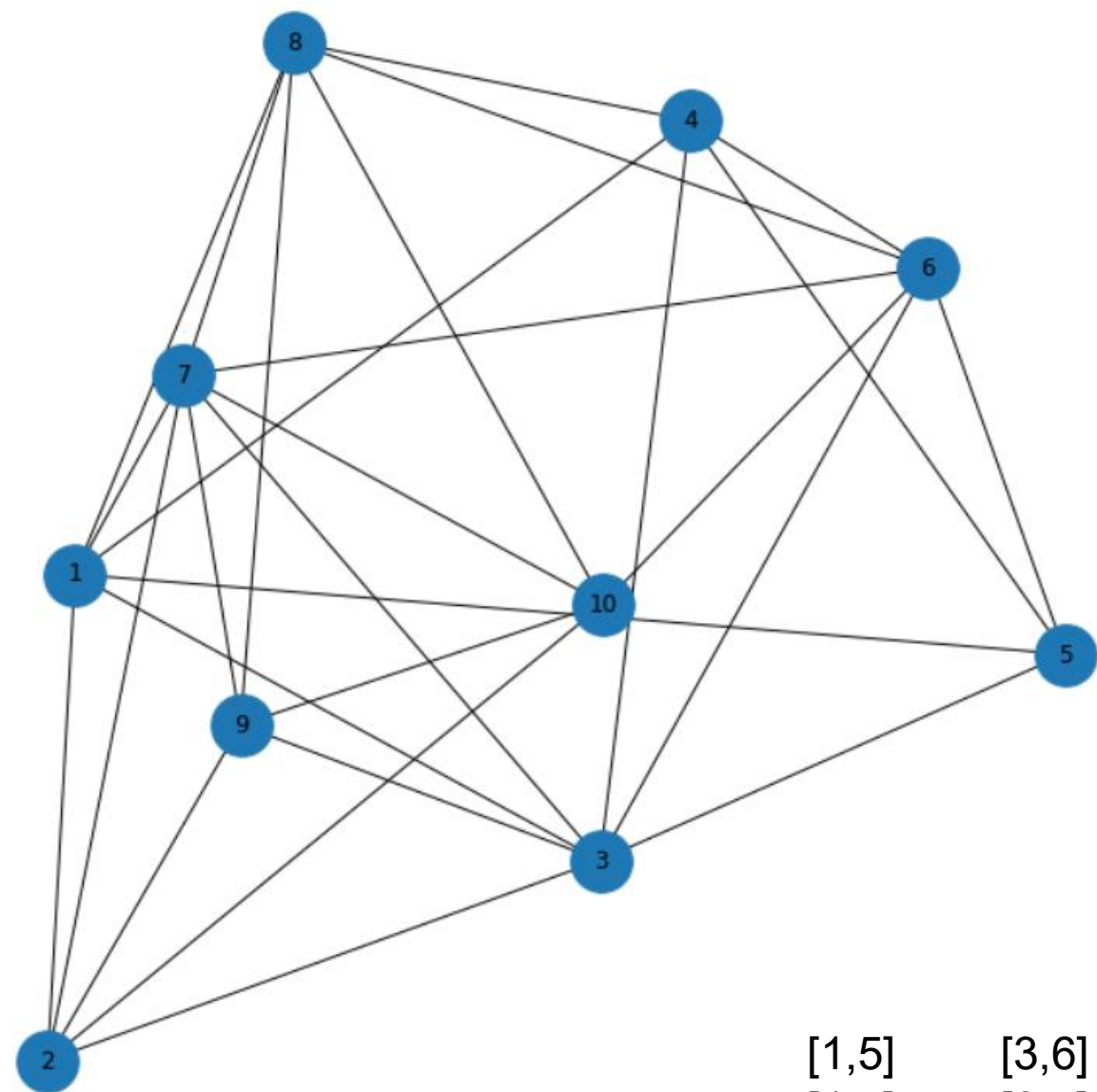
Number of nodes: 10

Number of edges: 18

Average degree: 3.6

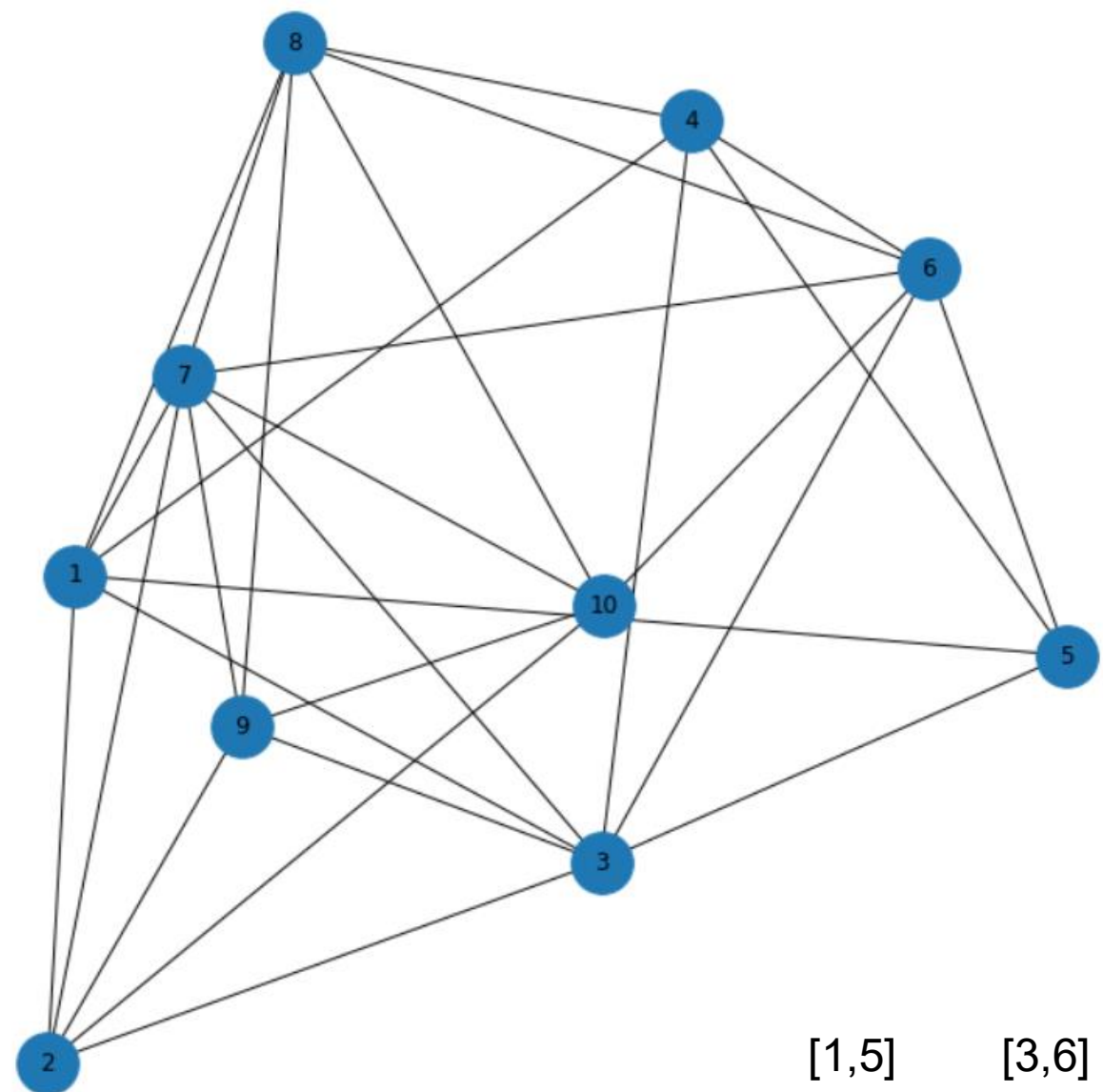
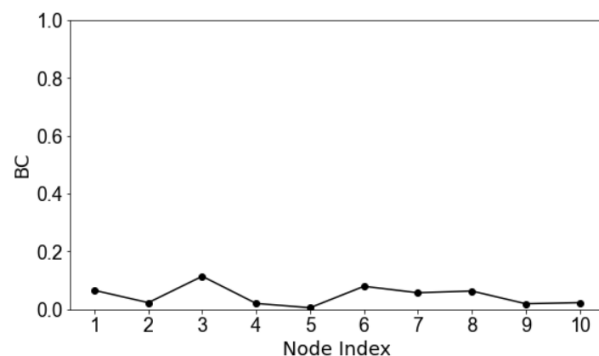
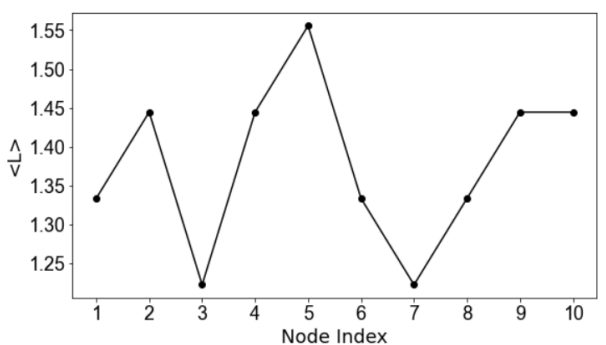
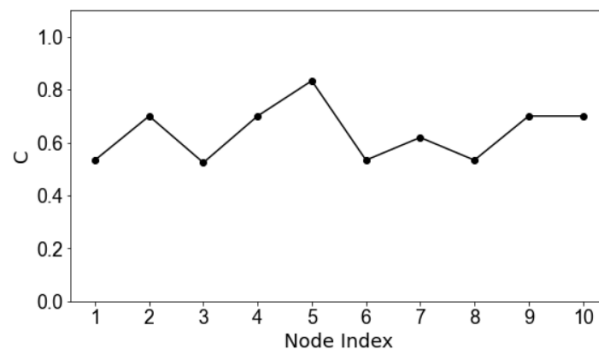
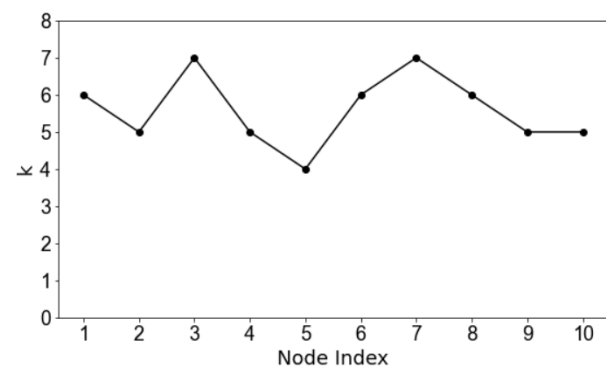
[3,7]

[4,8]



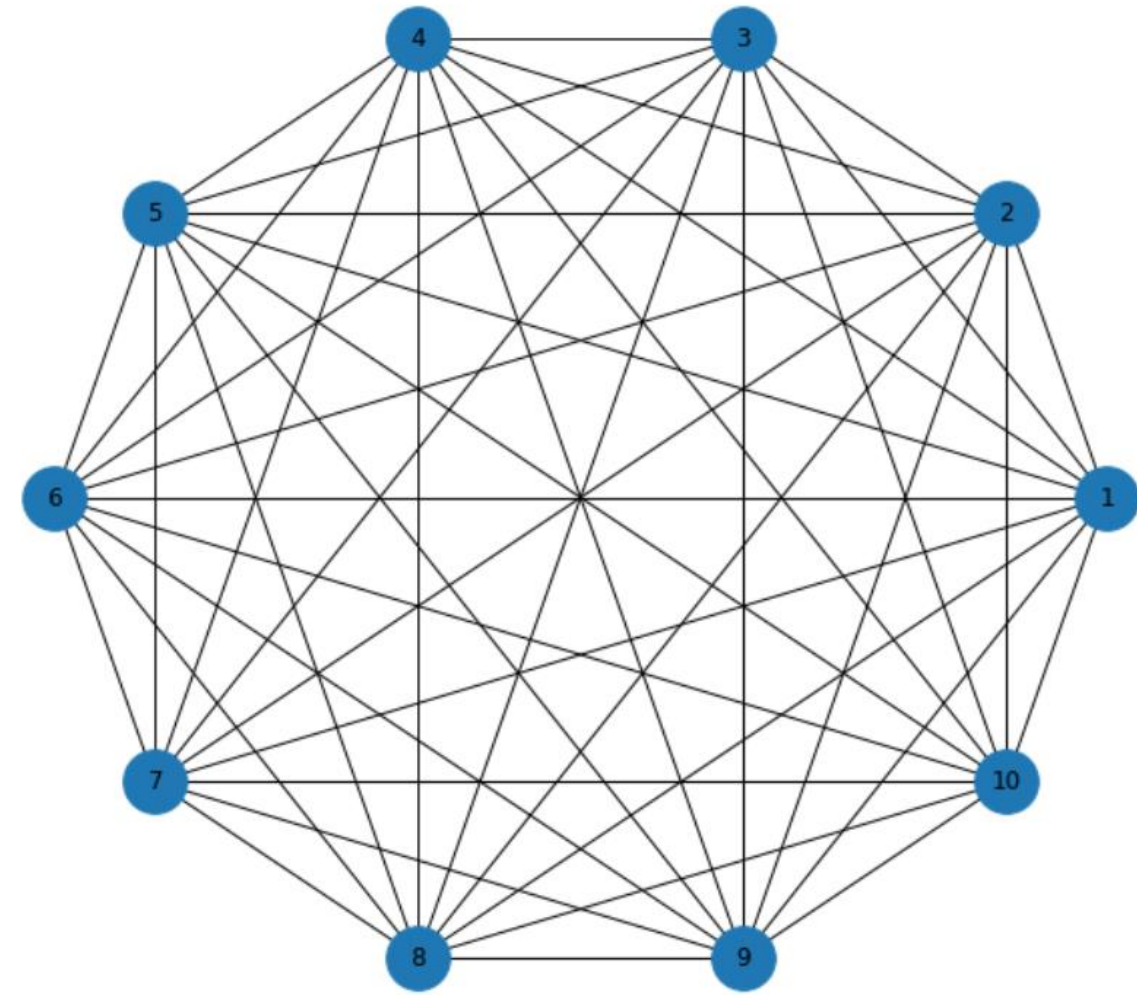
Number of nodes: 10
Number of edges: 28
Average degree: 5.6

[1,5]	[3,6]
[1,7]	[3,7]
[1,8]	[3,9]
[2,7]	[4,6]
[2,9]	[6,10]
[2,10]	



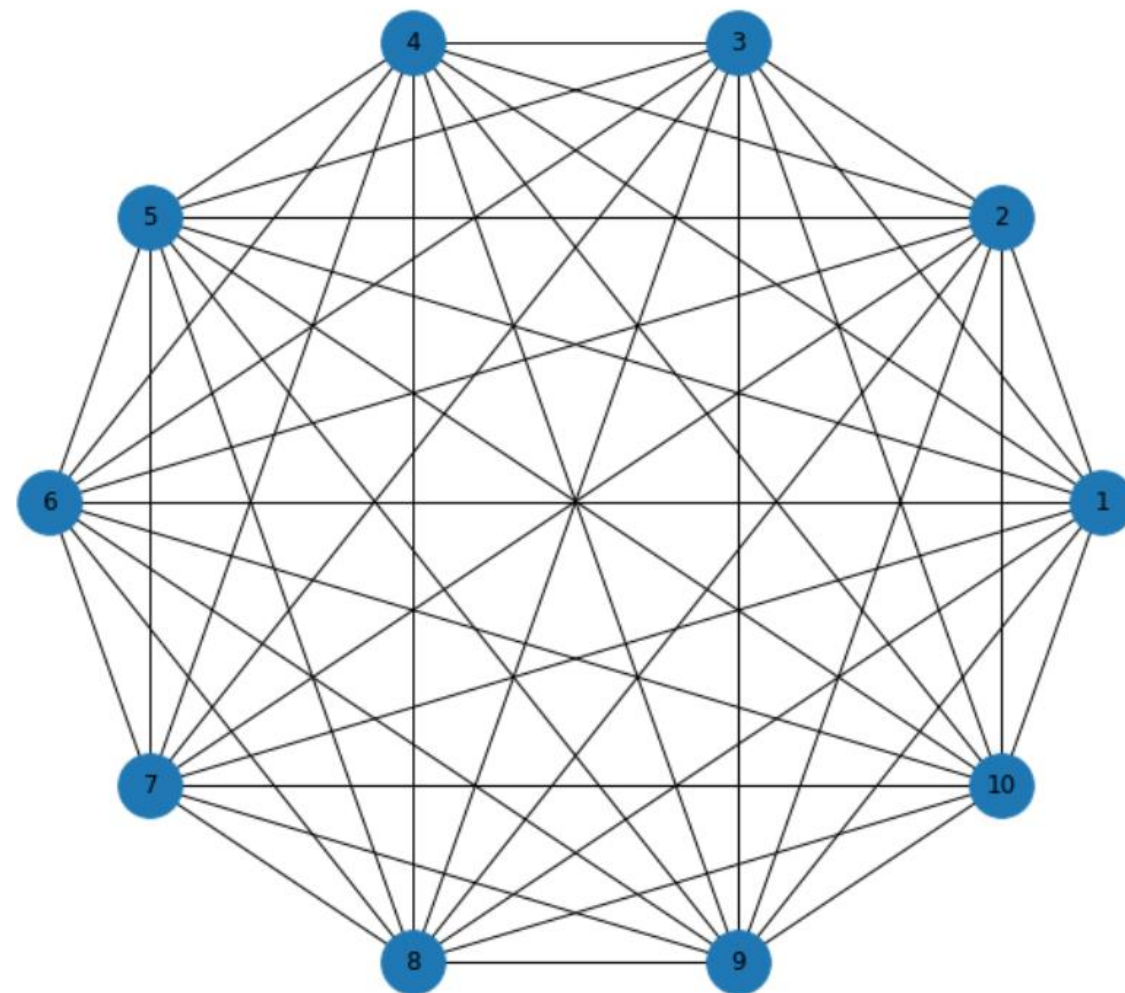
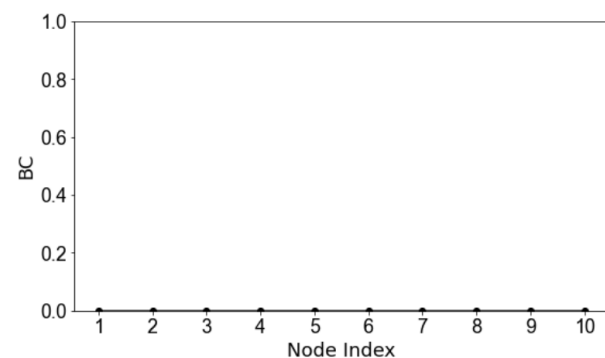
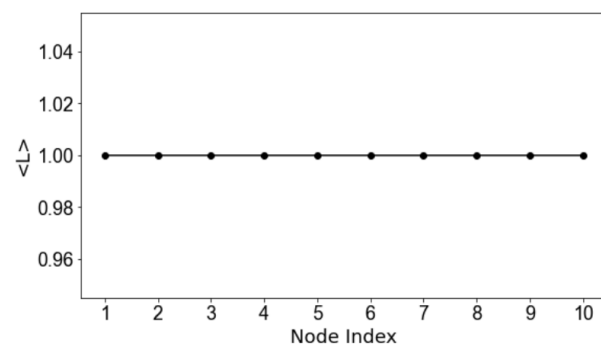
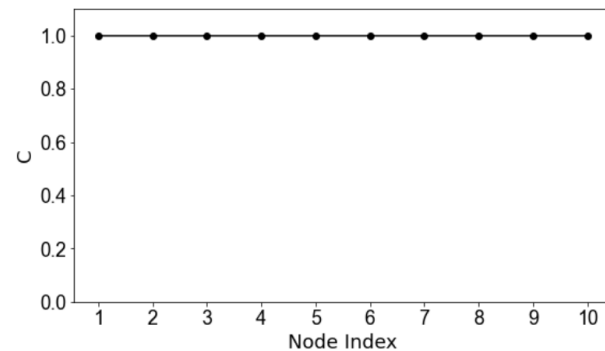
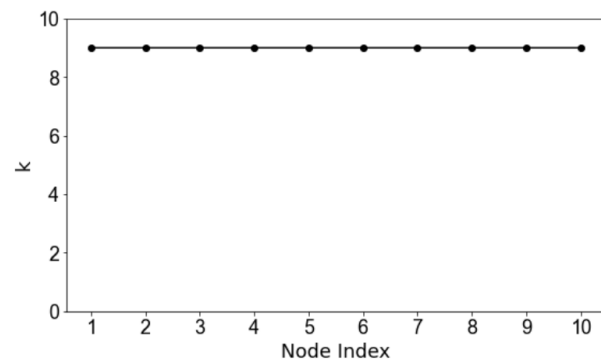
Number of nodes: 10
 Number of edges: 28
 Average degree: 5.6

[1,5] [3,6]
 [1,7] [3,7]
 [1,8] [3,9]
 [2,7] [4,6]
 [2,9] [6,10]
 [2,10]



Number of nodes: 10
Number of edges: 45
Average degree: 9

Complete network



Number of nodes: 10
 Number of edges: 45
 Average degree: 9

Complete network

Next lecture



Code for these toy graphs...

Thanks!



Co-funded by
the European Union



EuroHPC
Joint Undertaking

This project has received funding from the European High-Performance Computing Joint Undertaking (JU) under grant agreement No 101191697. The JU receives support from the Digital Europe Programme and Germany, Türkiye, Republic of North Macedonia, Montenegro, Serbia, Bosnia and Herzegovina.